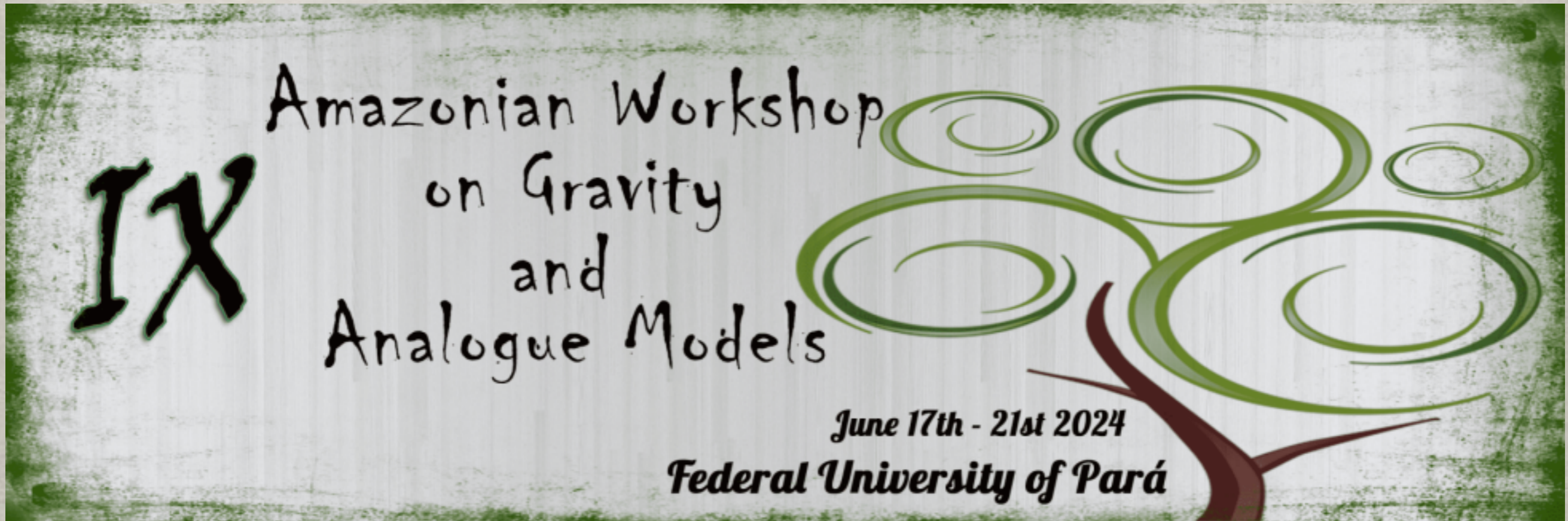


The wonderful world of compact objects with bosonic fields in GR



Carlos Herdeiro

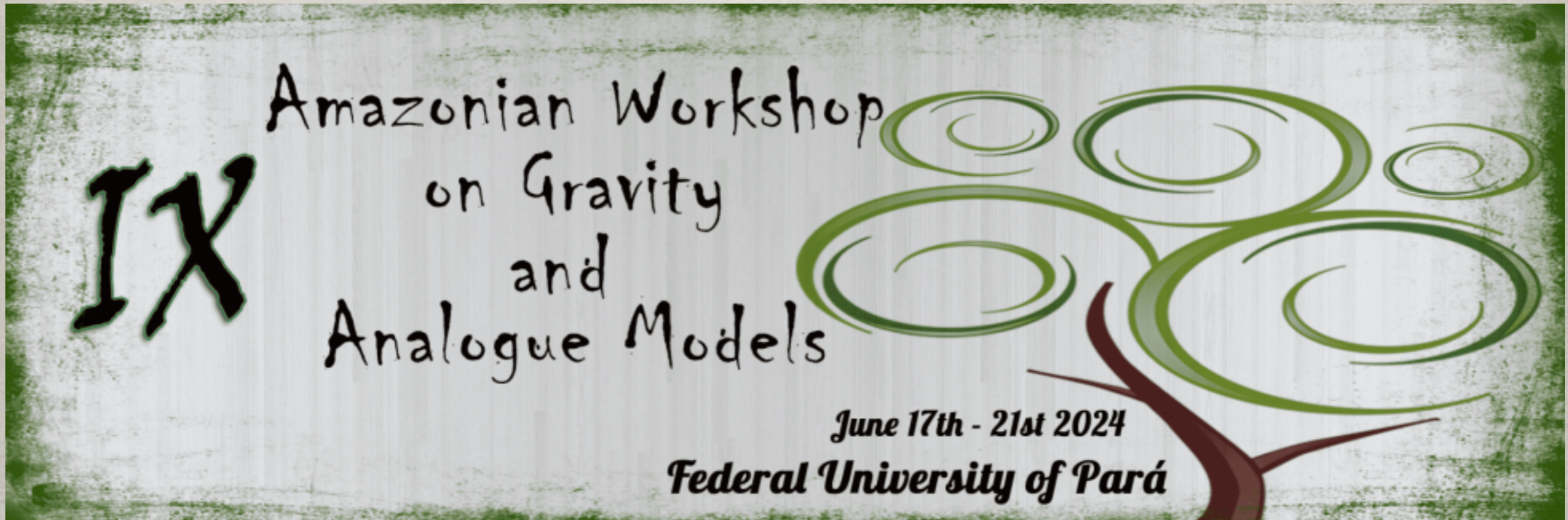
Gravitational Geometry and Dynamics Group, Aveiro University, Portugal

IX Amazonian Workshop on Gravity and Analogue Models

June 17, 2024

in collaboration with M. Brito, R. Brito, V. Cardoso, P. Cerda-Duran, P. Cunha, E. Costa-Filho, J. Degollado, J. Font, F. di Giovanni, J. Kunz, A. Moraes, I. Parapechka, E. Radu, N. Sanchis-Gual, N. Santos, Y. Shnir, M. Zilhão,...

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The paradigms and “tunnel vision”

Our understanding of the most compact objects in the Universe, in particular black holes, is **b(i)ased** by our paradigmatic models.

Einstein-Maxwell:

- Integrable (with symmetry):
analytic solutions;
- No solitons;
- No-hair for black holes (BHs):
uniqueness of Kerr-Newman BHs;
- No balanced neutral 2-BH systems
(asymptotically flat);

The paradigms and “tunnel vision”

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Einstein-(multi) Maxwell:

Einstein-(complex) Maxwell:

- Integrable (with symmetry): analytic solutions;
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Einstein-(massive, complex) Maxwell

Einstein-(massive, complex) Klein-Gordon:

- No integrable structure known: numerical solutions;
- Landscape of solitons: bosonic stars (BSs) with some dynamical surprises;

TODAY!!

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- Hairy BHs and non-uniqueness; deep relations to superradiance and BSs;

Kerr Black Holes with Scalar Hair

Carlos A. R. Herdeiro and Eugen Radu

Departamento de Física da Universidade de Aveiro and I3N, Campus de Santiago, 3810-183 Aveiro, Portugal

(Received 13 March 2014; revised manuscript received 23 April 2014; published 2 June 2014)

We present a family of solutions of Einstein's gravity minimally coupled to a complex, massive scalar field, describing asymptotically flat, spinning black holes with scalar hair and a regular horizon. These hairy black holes (HBHs) are supported by rotation and have no static limit. Besides mass M and angular momentum J , they carry a conserved, continuous Noether charge Q measuring the scalar hair. HBHs branch off from the Kerr metric at the threshold of the superradiant instability and reduce to spinning boson stars in the limit of vanishing horizon area. They overlap with Kerr black holes for a set of (M, J) values. A single Killing vector field preserves the solutions, tangent to the null geodesic generators of the event horizon. HBHs can exhibit sharp physical differences when compared to the Kerr solution, such as $J/M^2 > 1$, a quadrupole moment larger than J^2/M , and a larger orbital angular velocity at the innermost stable circular orbit. Families of HBHs connected to the Kerr geometry should exist in scalar (and other) models with more general self-interactions.

DOI: [10.1103/PhysRevLett.112.221101](https://doi.org/10.1103/PhysRevLett.112.221101)

PACS numbers: 04.70.Bw, 03.50.-f

E. Radu's
and
L. Leite's
talks

Hairy BHs in GR with matter obeying all important energy conditions which have a physical formation mechanism.

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- Balanced neutral black holes (asymptotically flat)

Two Spinning Black Holes Balanced by Their Synchronized Scalar Hair

Carlos A. R. Herdeiro[✉] and Eugen Radu

Departamento de Matemática da Universidade de Aveiro and CIDMA, Campus de Santiago, 3810-183 Aveiro, Portugal

 (Received 30 May 2023; accepted 8 August 2023; published 21 September 2023)

General relativity minimally coupled to a massive, free, complex scalar field, is shown to allow asymptotically flat solutions, nonsingular on and outside the event horizon, describing two spinning black holes (2sBHs) in equilibrium, with coaxial, aligned angular momenta. The 2sBHs configurations bifurcate from solutions describing dipolar spinning boson stars. The BHs emerge at equilibrium points diagnosed by a test particle analysis and illustrated by a Newtonian analog. The individual BH “charges” are mass and angular momentum only. Equilibrium is due to the scalar *environment*, acting as a (compact) dipolar field, providing a lift against their mutual attraction, making the 2sBHs (h)airborne. We explore the 2sBHs domain of solutions and its main features.

DOI: [10.1103/PhysRevLett.131.121401](https://doi.org/10.1103/PhysRevLett.131.121401)

C. Macedo's
talk

The hair can provide a physical mechanism to balance two neutral asymptotically flat spinning black holes, without conical singularities, which was an old problem in GR.

Plan of this talk:

**Einstein-(multi) Maxwell:
Einstein-(complex) Maxwell:**

- Integrable (with symmetry):
analytic solutions;
- No solitons;
- No-hair for black holes (BHs):
uniqueness of Kerr-Newman BHs;
- No balanced neutral black holes
(asymptotically flat);

**Einstein-(massive, complex) Maxwell
Einstein-(massive, complex) Klein-Gordon:**

- No integrable structure known:
numerical solutions;
- I) Landscape of solitons: bosonic stars (BSs)
with some dynamical surprises;
- II) Hairy BHs and non-uniqueness; deep
relations to superradiance and BSs;
- III) Balanced neutral black holes
(asymptotically flat)

I) Landscape of solitons:
bosonic stars (BSs) with some dynamical surprises

G. Raposo's
course

and

G. Olmo's
talk

Bosonic stars (a macro perspective):

- Appear in General Relativity with simple and physically reasonable matter sources: complex massive scalar fields or vector fields, possibly with self-interactions, but certainly with a mass term.

Massive-complex-scalar-vacuum:

Scalar Boson Stars

$$\mathcal{S} = \frac{1}{4\pi} \int d^4x \sqrt{-g} \left(\frac{R}{4} - \nabla_\alpha \Phi^* \nabla^\alpha \Phi - \mu^2 |\Phi|^2 \right)$$

New scale

“Reference models”

Massive-complex-vector-vacuum:

Vector Boson Stars
or
Proca Stars

$$\mathcal{S} = \int d^4x \sqrt{-g} \left(\frac{1}{16\pi G} R - \frac{1}{4} \mathcal{F}_{\alpha\beta} \bar{\mathcal{F}}^{\alpha\beta} - \frac{1}{2} \mu^2 \mathcal{A}_\alpha \bar{\mathcal{A}}^\alpha \right) .$$

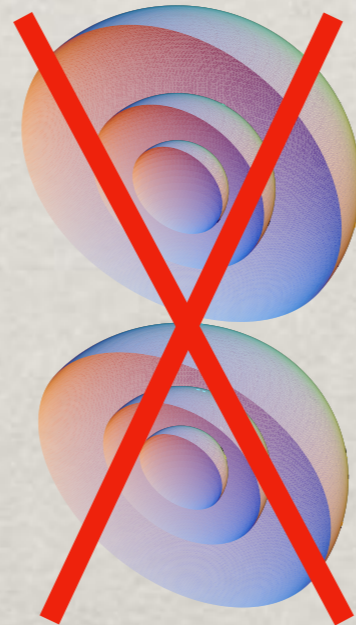
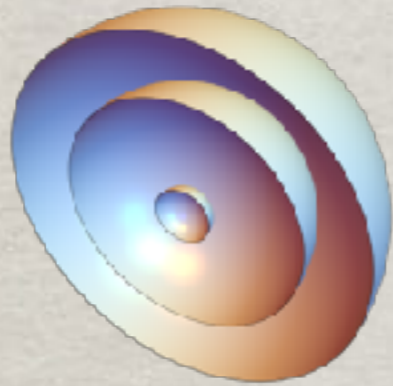
New scale

A surprising (dynamically) different picture:

Static:

Spinning:

Scalar

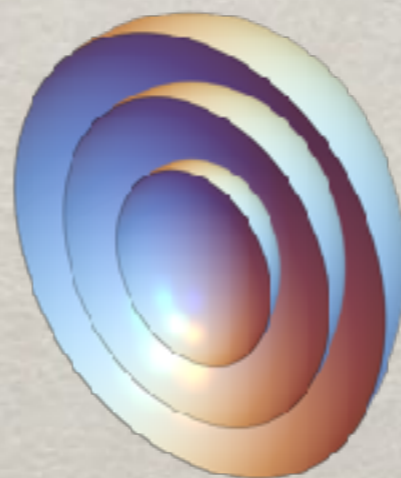


Monopole

Dipole

Toroidal

Vector



Spheroidal



Bosonic stars (a micro perspective):

- They are a Bose-Einstein condensate of many ultralight particles in the same quantum state, thus justifying the classical description. [CH, Radu, 2205.05395](#)
- The need for ultralightness comes from the existence of a (model dependent) maximal mass for the bosonic stars:

$$M_{\text{ADM}}^{\text{max}} \simeq \alpha_{\text{BS}} \frac{M_{\text{Pl}}^2}{\mu} \simeq \alpha_{\text{BS}} 10^{-19} M_{\odot} \left(\frac{\text{GeV}}{\mu} \right)$$

- Thus, for bosonic stars with masses in the astrophysical black holes range the fundamental bosonic particle must be ultralight:

$$M_{\text{ADM}}^{\text{max}} \sim (1 - 10^{10}) M_{\odot} \quad \longleftrightarrow \quad \mu \sim (10^{-10} - 10^{-20}) \text{ eV}$$

- If such hypothetical particle(s) have feeble or no-interactions with standard model constituents, they are fuzzy dark matter, only detectable gravitationally.

[Suárez, Robles, Matos, 1302.0903; Hui, Ostriker, Tremain and Witten, 1610.08297](#)

But what is their HEP origin? Axiverse? [Arvanitaki et al., 0905.4720](#)

Something else? [Freitas et al. JCAP 12 \(2021\) 047](#)

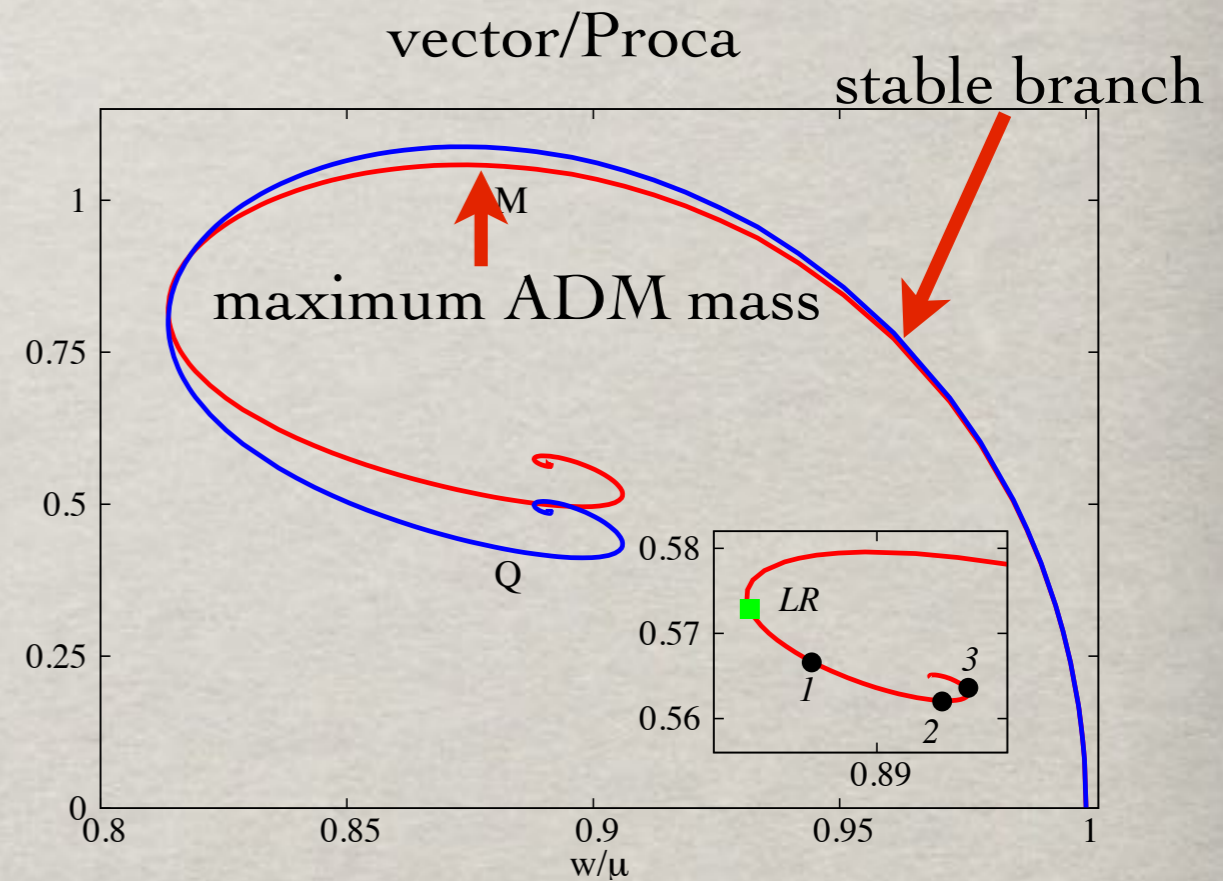
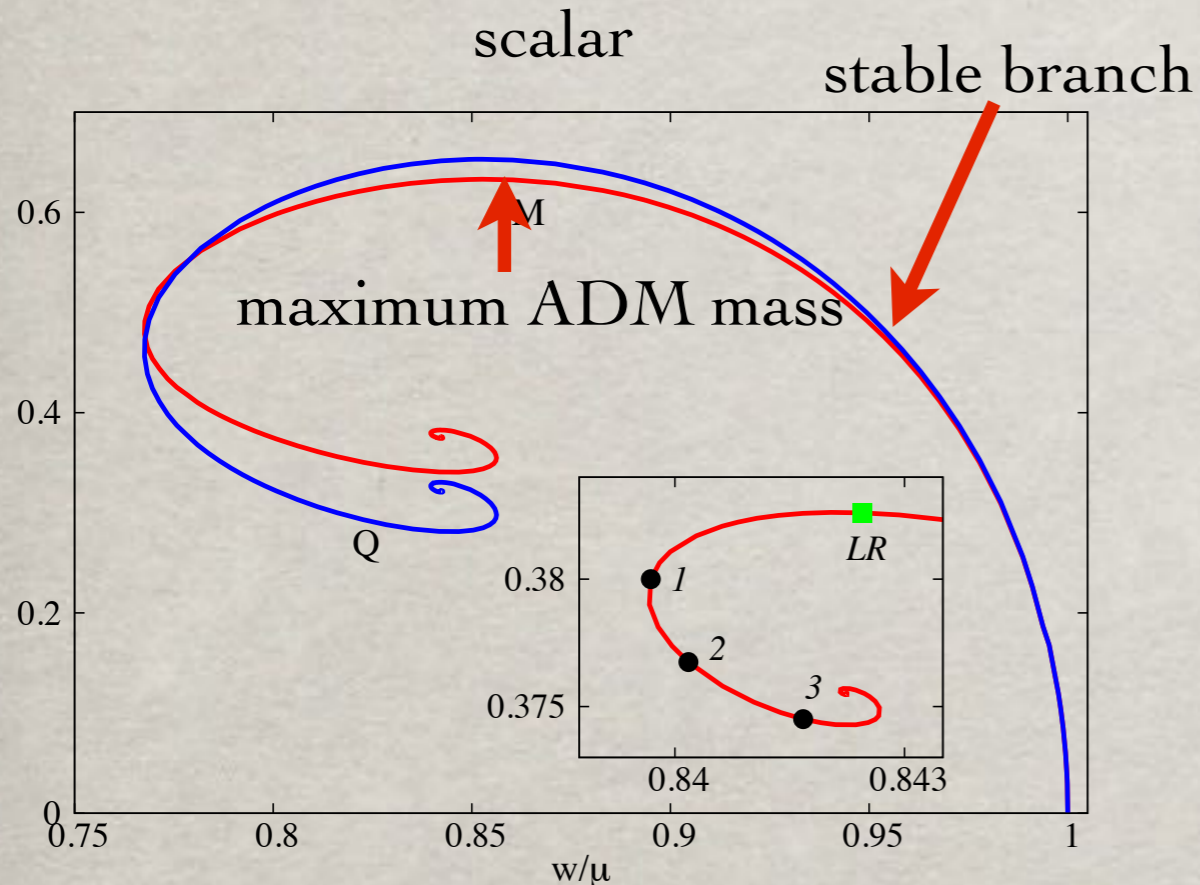
Spherical bosonic stars - stability

Kaup, Phys. Rev. 172 (1968) 1331; Ruffini and Bonazzola, Phys. Rev. 187 (1969) 1767;
 Brito, Cardoso, CH and Radu, PLB 752 (2016) 291; CH, Pombo, Radu, PLB 773 (2017) 654

$$\Phi = \phi(r)e^{-i\omega t}$$

$$\mathcal{A} = e^{-i\omega t} [f(r)dt + ig(r)dr]$$

frequency

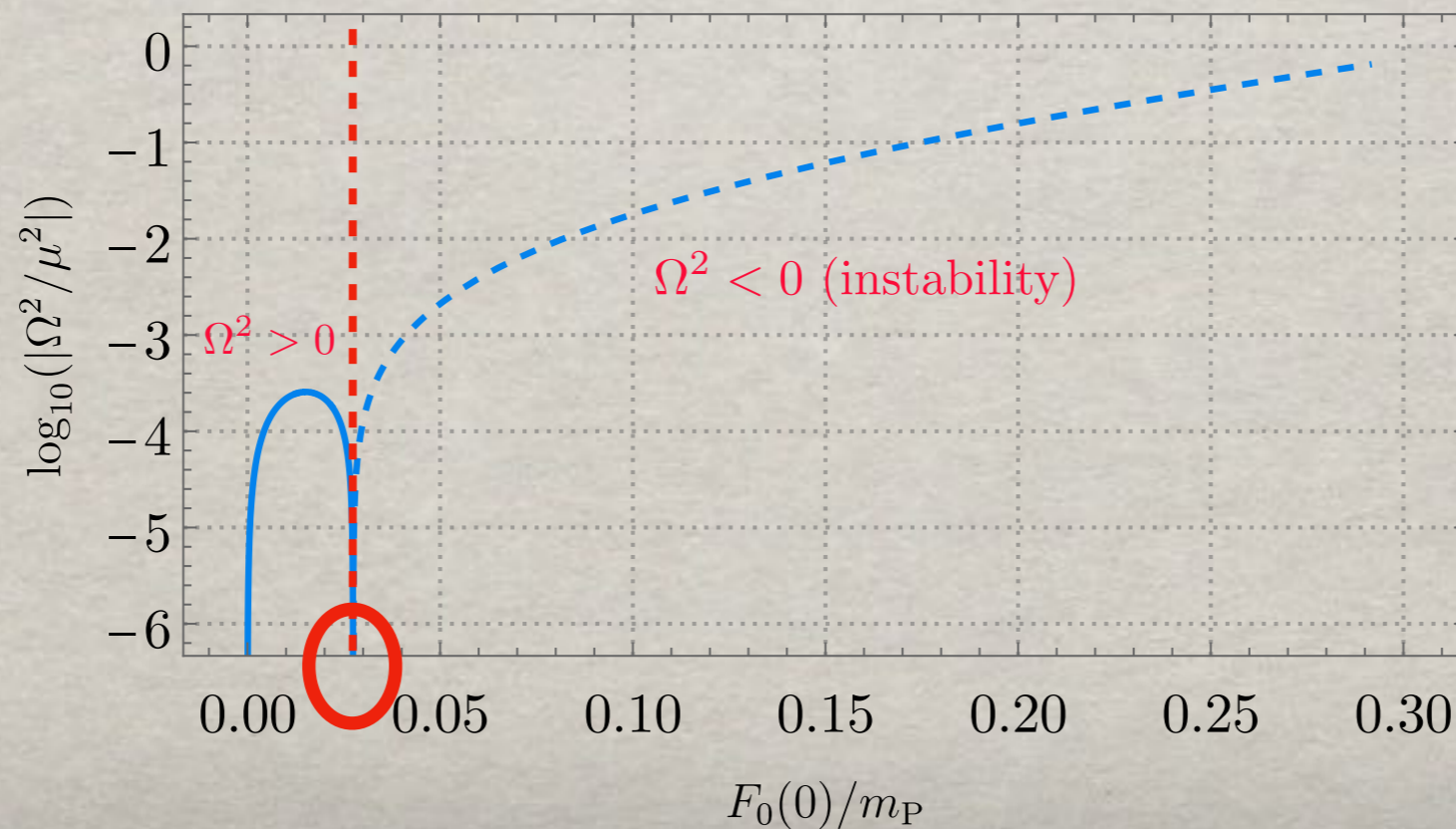
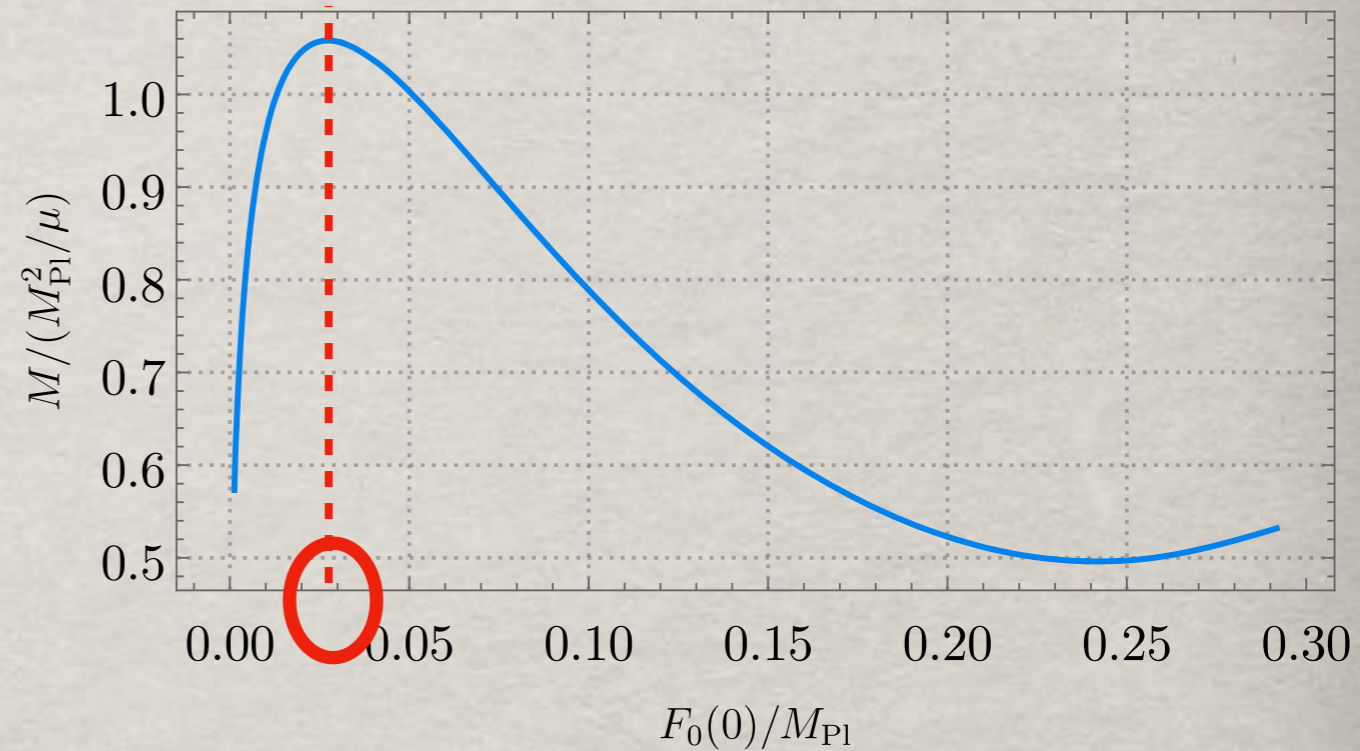
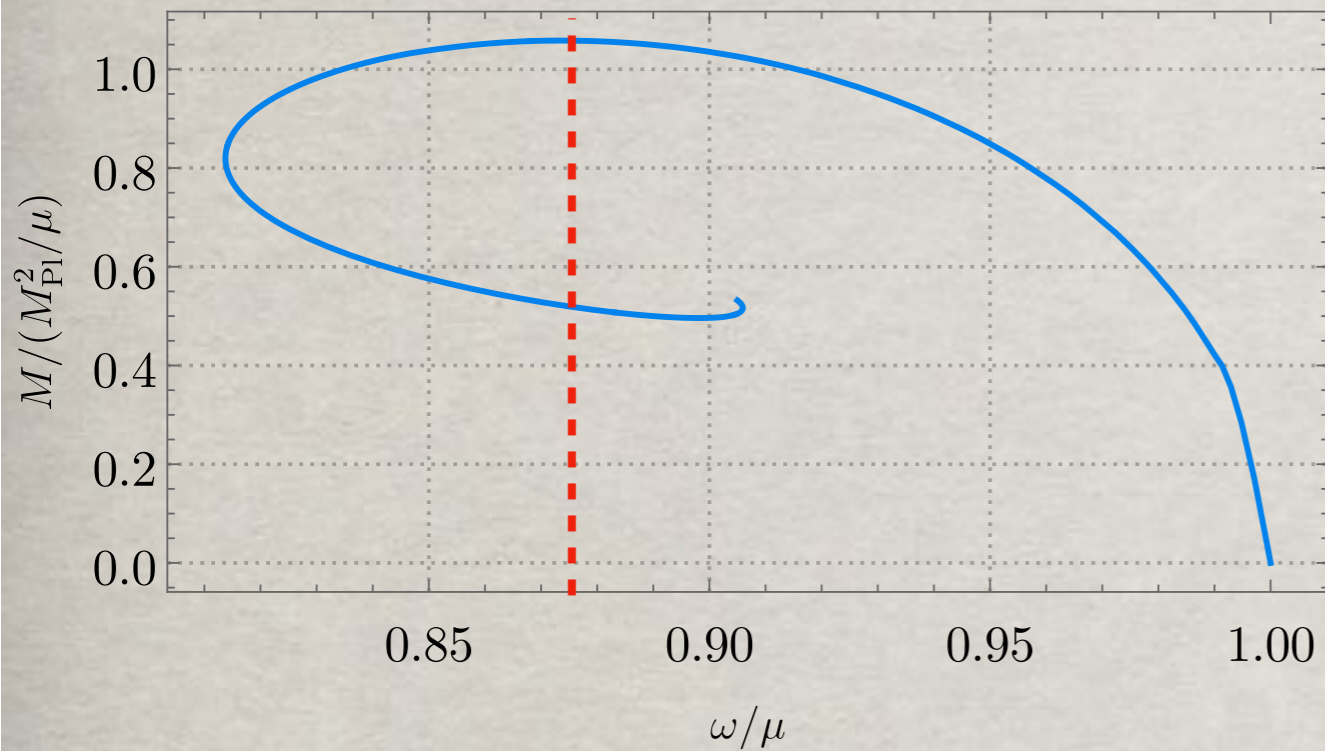


Studying linearized radial perturbations of the coupled system shows that an unstable mode arises precisely at the maximum of the ADM mass *M. Gleiser and R. Watkins, NPB 319 (1989) 733; T. D. Lee and Y. Pang, NPB 315, 477 (1989); Brito, Cardoso, CH and Radu, PLB 752 (2016) 291.*

Unstable BSs can migrate, decay into a Schwarzschild black hole or disperse entirely *Seidel and Suen, PRD 42 (1990) 384; Guzman, PRD 70 (2004) 044033; Hawley and Choptuik, PRD 62 (2000) 104024; Sanchis-Gual, CH, Radu, Degollado, Font, PRD 95 (2017) 104028*

Spherical perturbation theory of mini-Proca stars:

Santos, Benone and CH (2404.07257)



C. Benone's
talk

Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Bosonic stars can have a multipolar distribution

CH, Kunz, Parapechka, Radu, Shnir, PLB 812 (2021) 136027

$$\square\Phi = \mu^2\Phi$$

$$\Phi = e^{-i\omega t} \sum_{\ell,m} R_\ell(r) Y_{\ell m}(\theta, \varphi)$$

$$R_\ell(r) = \frac{c}{\sqrt{r}} K_{\frac{1}{2}+\ell}(r\sqrt{\mu^2 - \omega^2})$$

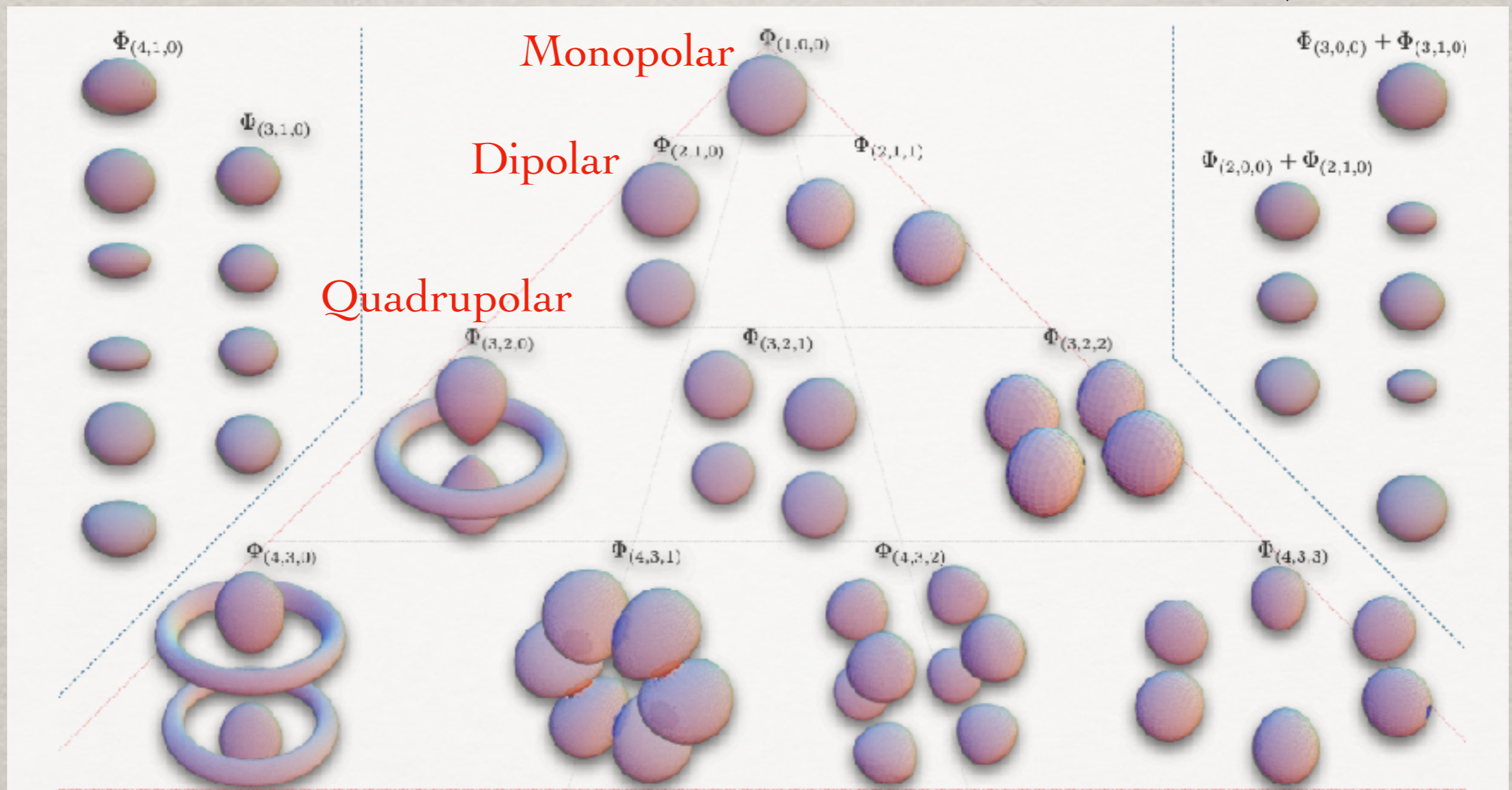


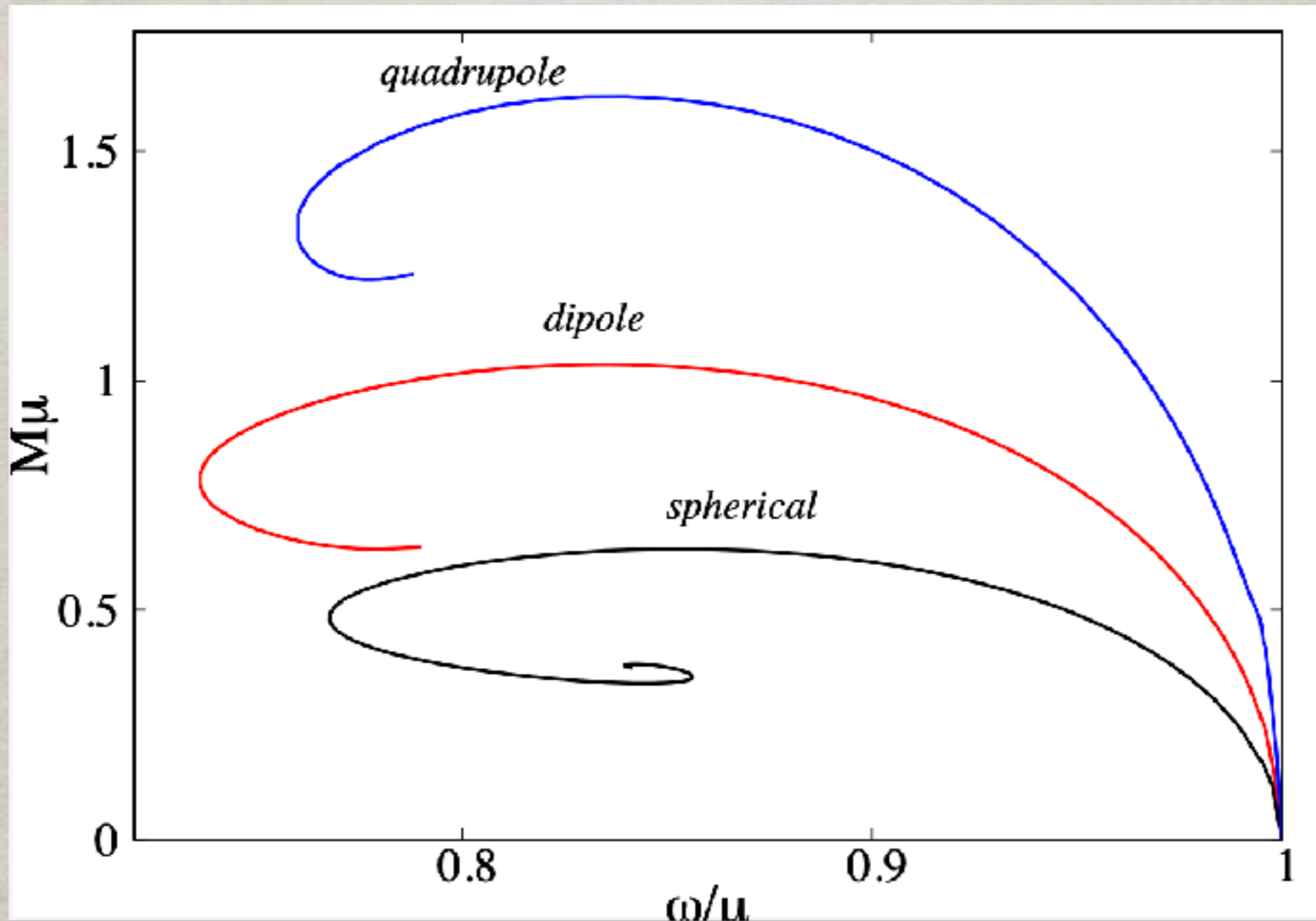
FIG. 3. Surfaces of constant energy density for a selection of $\Phi_{(N,\ell,m)}$. The hydrogen orbitals-like morphology is unmistakable, see *e.g.* [2].

Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Bosonic stars can have a multipolar distribution

CH, Kunz, Parapechak, Radu, Shnir, PLB 797 (2019) 134845

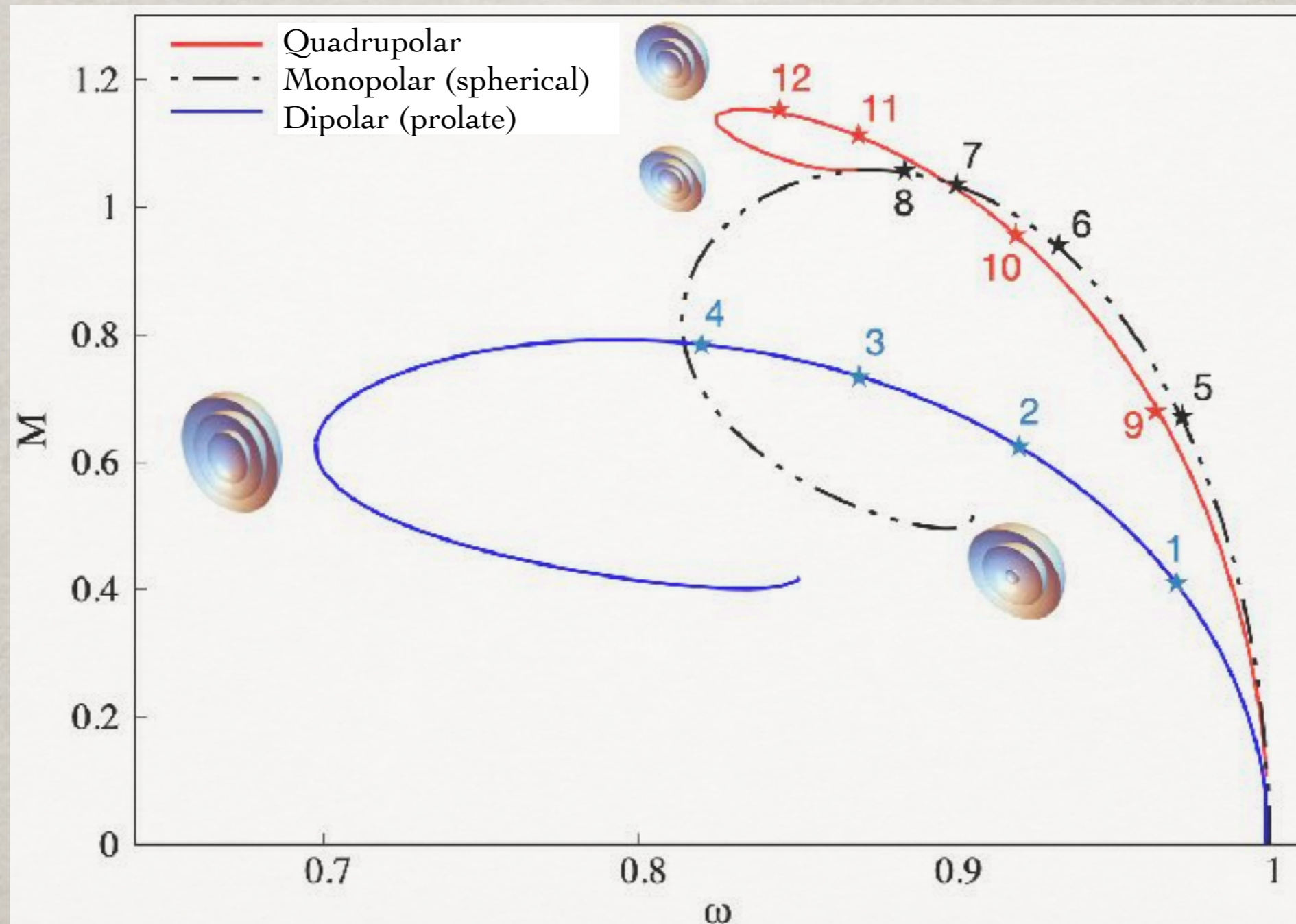


Cunha, CH, Kunz, Radu, Shnir, PRD 106 (2022) 124039

Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Evidence 1: - energetics (the ground state)



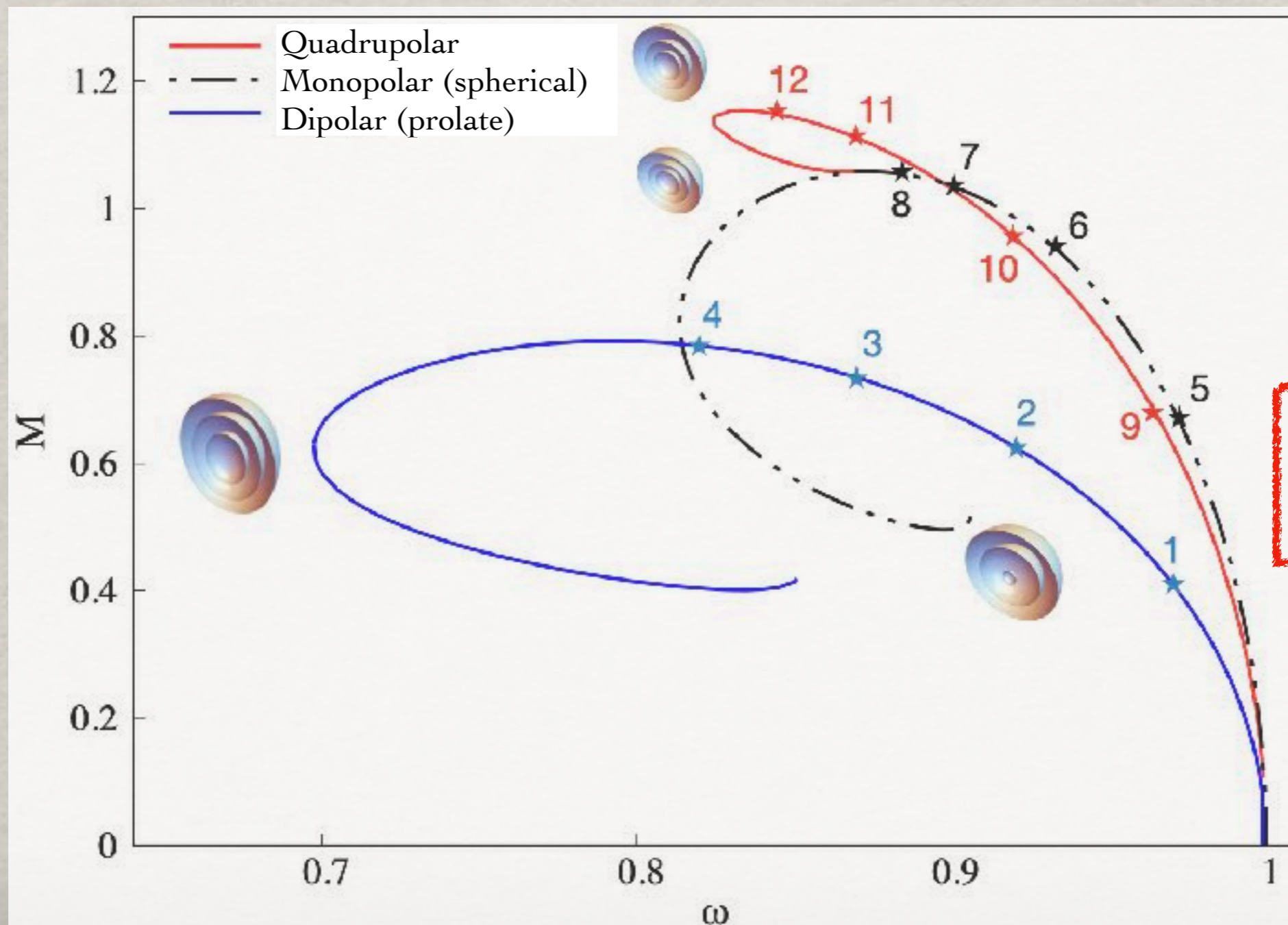
Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Evidence 2: - dynamics (using 3D NR simulations)

see e.g. Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101

Q1) if the dipolar Proca stars are the ground state, are they stable in a long term numerical evolution?



M. Zilhão's course

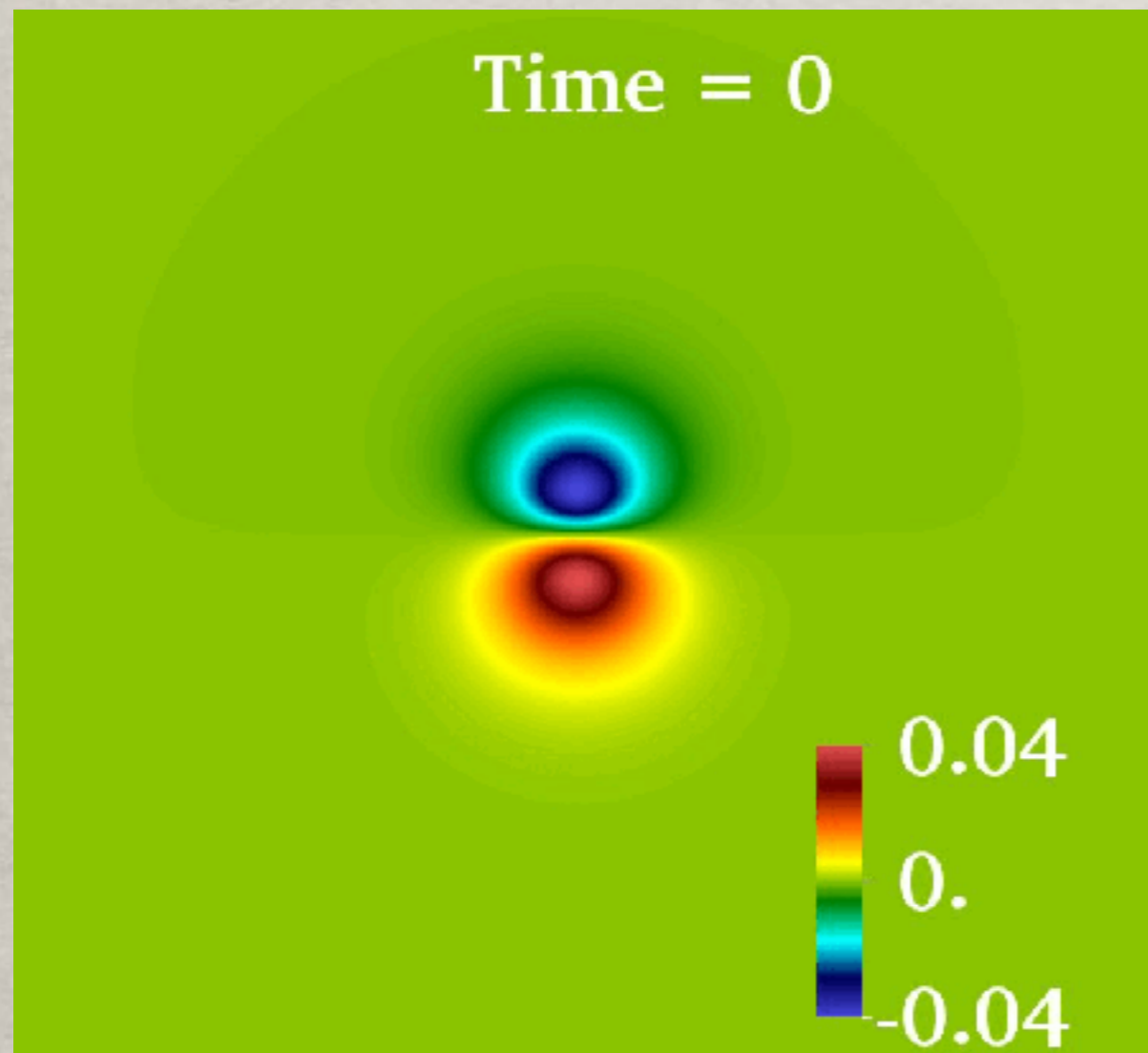
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Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

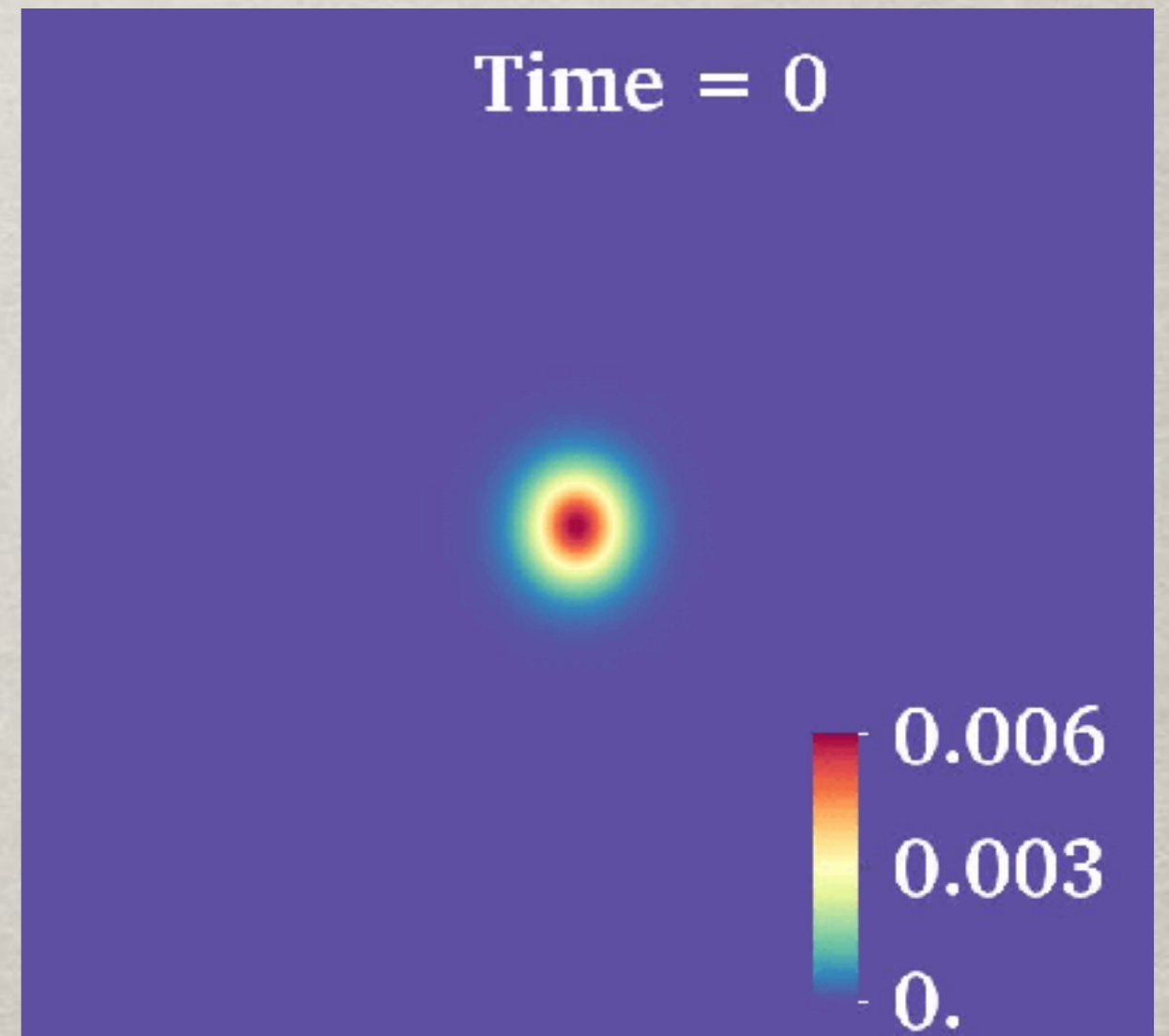
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Proca (scalar) potential x-z plane



Energy density x-z plane

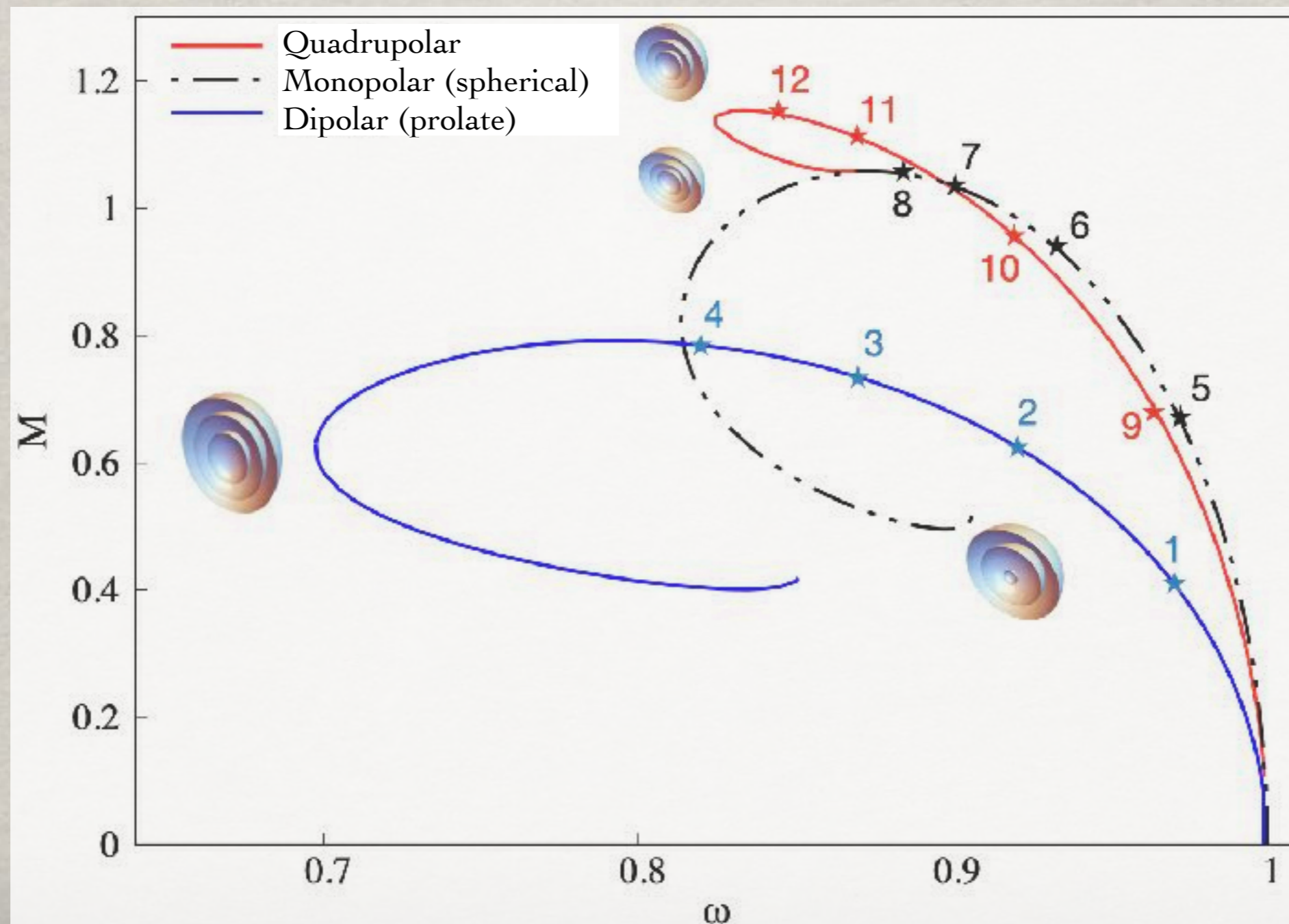
Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Evidence 2: - dynamics (using 3D NR simulations)

see e.g. Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101

Q2) if the dipolar Proca stars are the ground state, are spherical stars unstable?



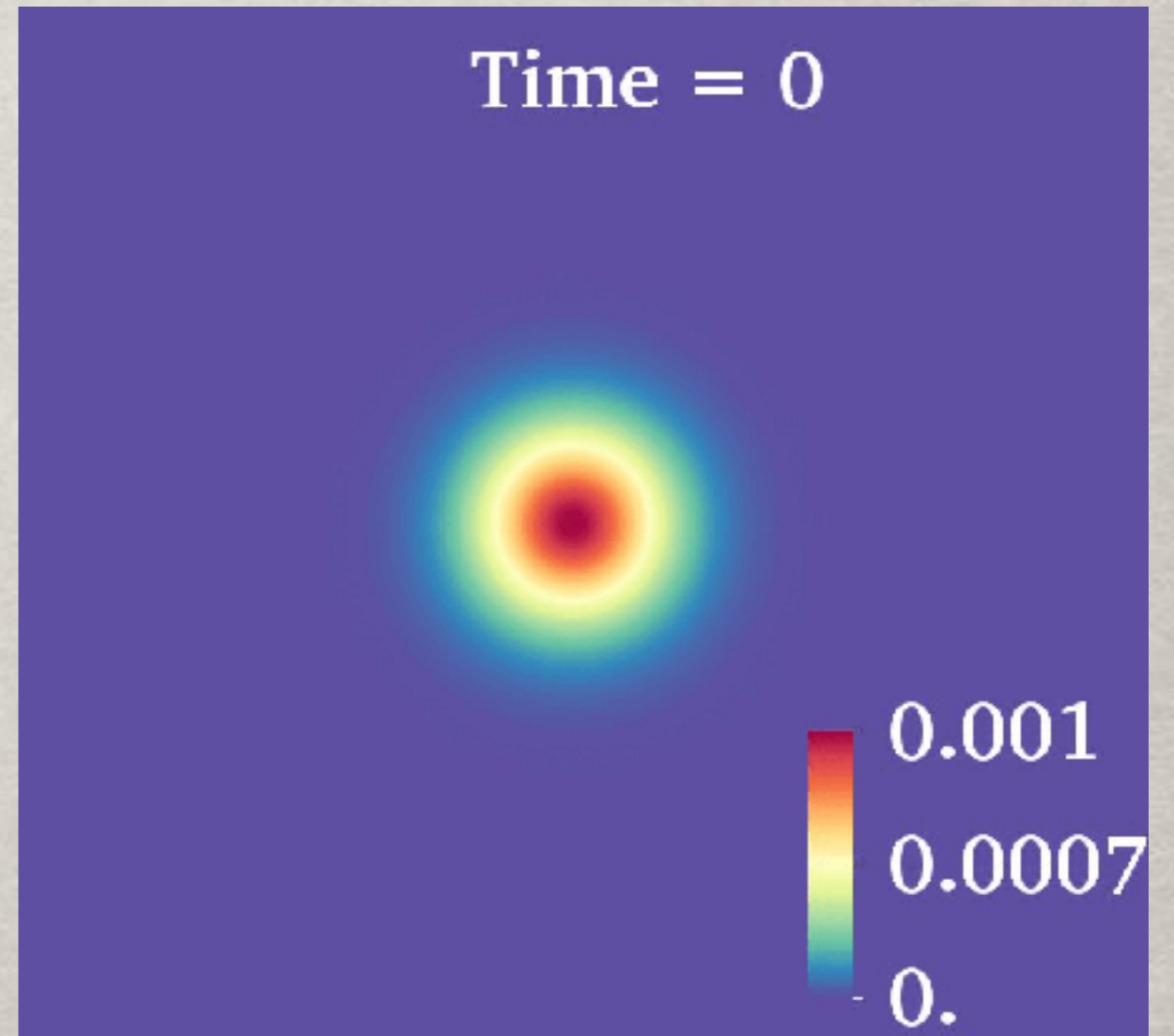
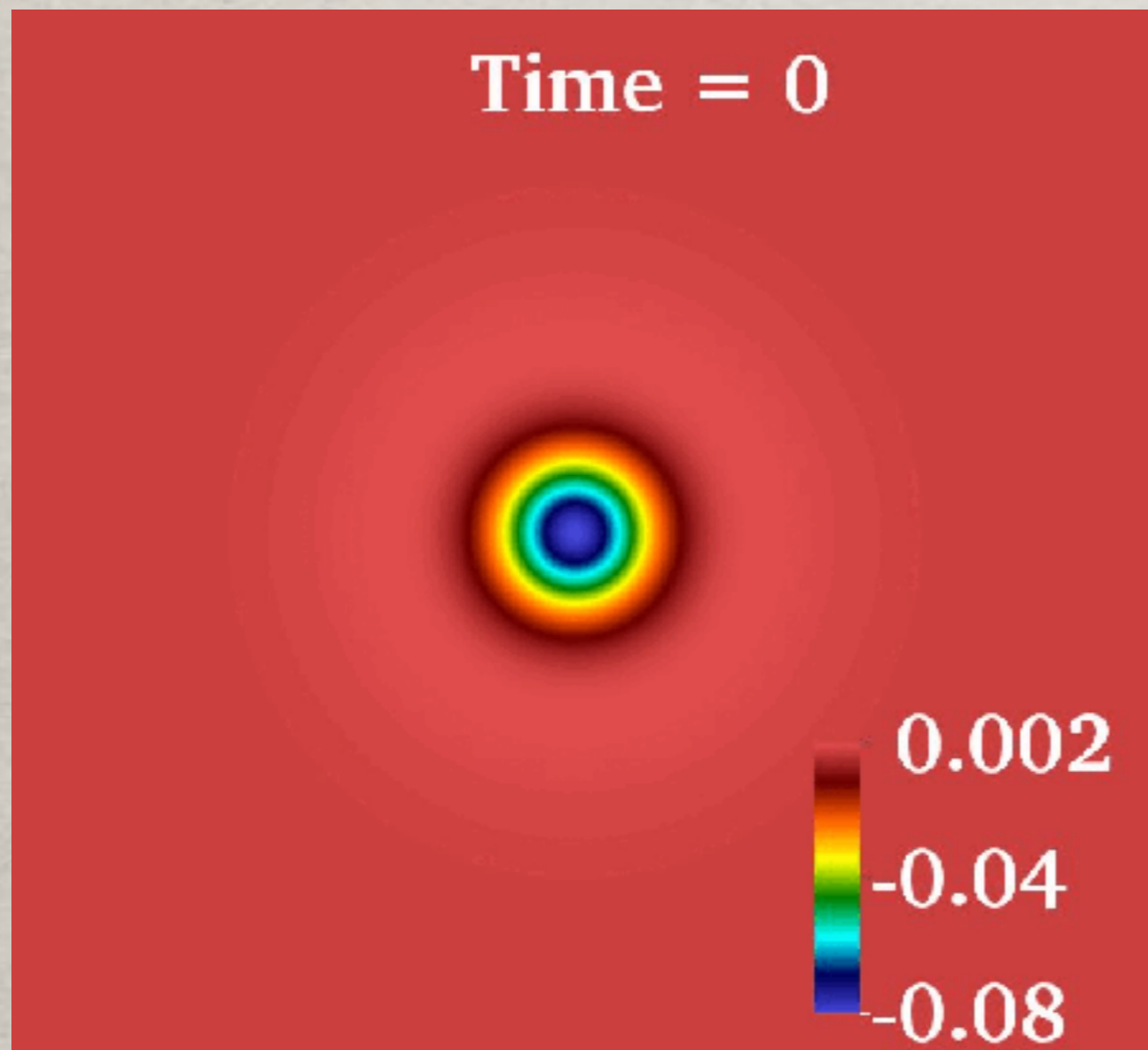
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see e.g. Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101

Prolate (P)	Spherical (S)	Quadrupolar (Q)
1 -(0.970,0.4124) <i>Stable</i>	5 -(0.970,0.6928) $S \rightarrow P ; [\mathbb{Z}_2]$	9 -(0.965,0.6928) $Q \rightarrow P ; [\mathbb{Z}_2]$ <i>Stable</i>
2 -(0.920,0.6261) <i>Stable</i>	6 -(0.936,0.9245) $S \rightarrow P ; [\mathbb{Z}_2]$ $s \rightarrow Q \rightarrow P$	10 -(0.920,0.9549) $Q \rightarrow P ; [\mathbb{Z}_2]$ <i>Stable</i>
3 -(0.870,0.7346) <i>Stable</i>	7 -(0.900,1.035) $S \rightarrow P ; [\mathbb{Z}_2]$ $s \rightarrow Q \rightarrow P$	11 -(0.870,1.1108) $Q \rightarrow BH ; [\mathbb{Z}_2]$ <i>Stable</i>
4 -(0.820, 0.7846) <i>Stable</i>	8 -(0.885,1.054) $S \rightarrow P ; [\mathbb{Z}_2]$ $S \rightarrow Q$	12 -(0.845,1.1478) $Q \rightarrow BH ; [\mathbb{Z}_2]$ <i>Stable</i>

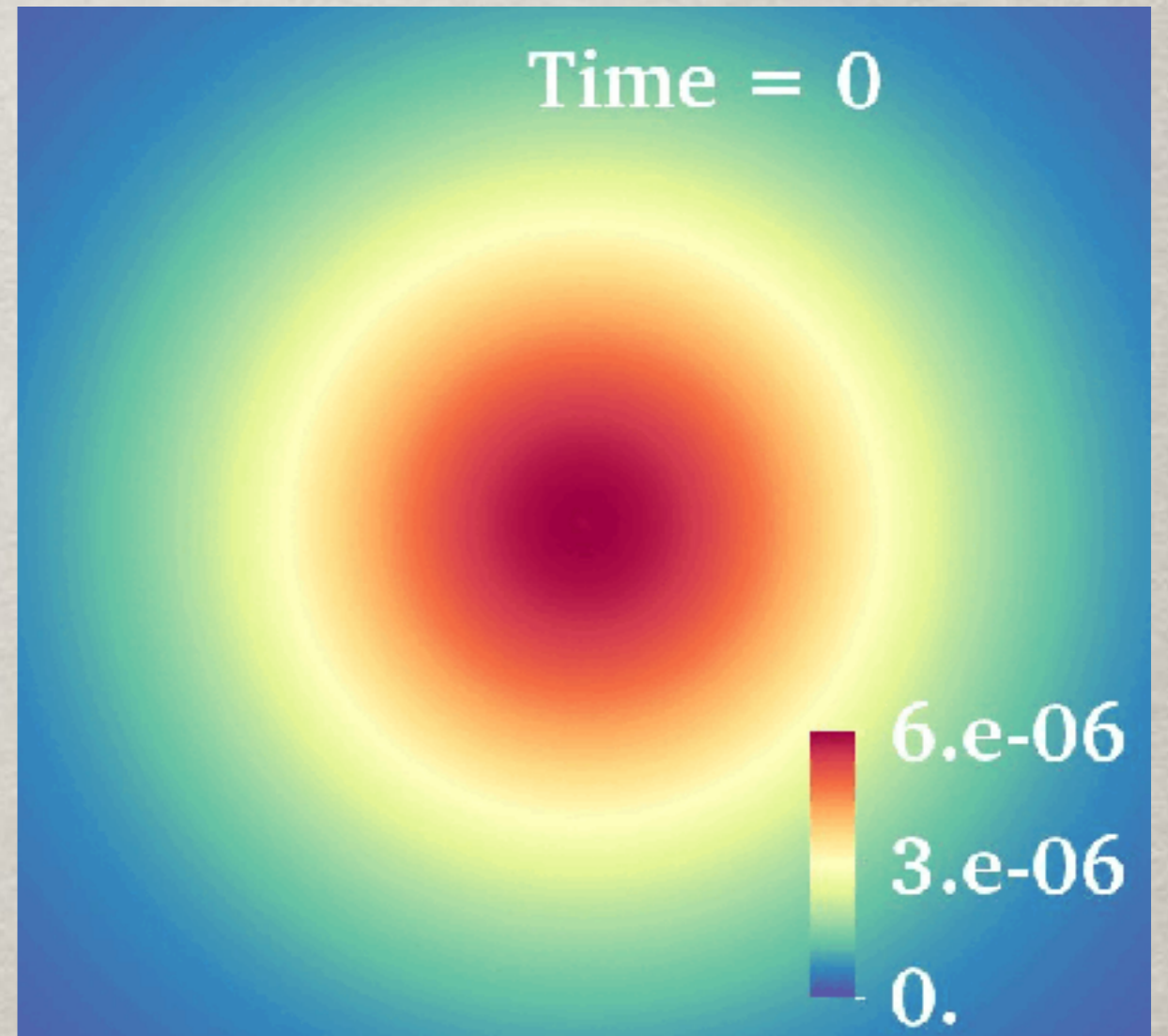
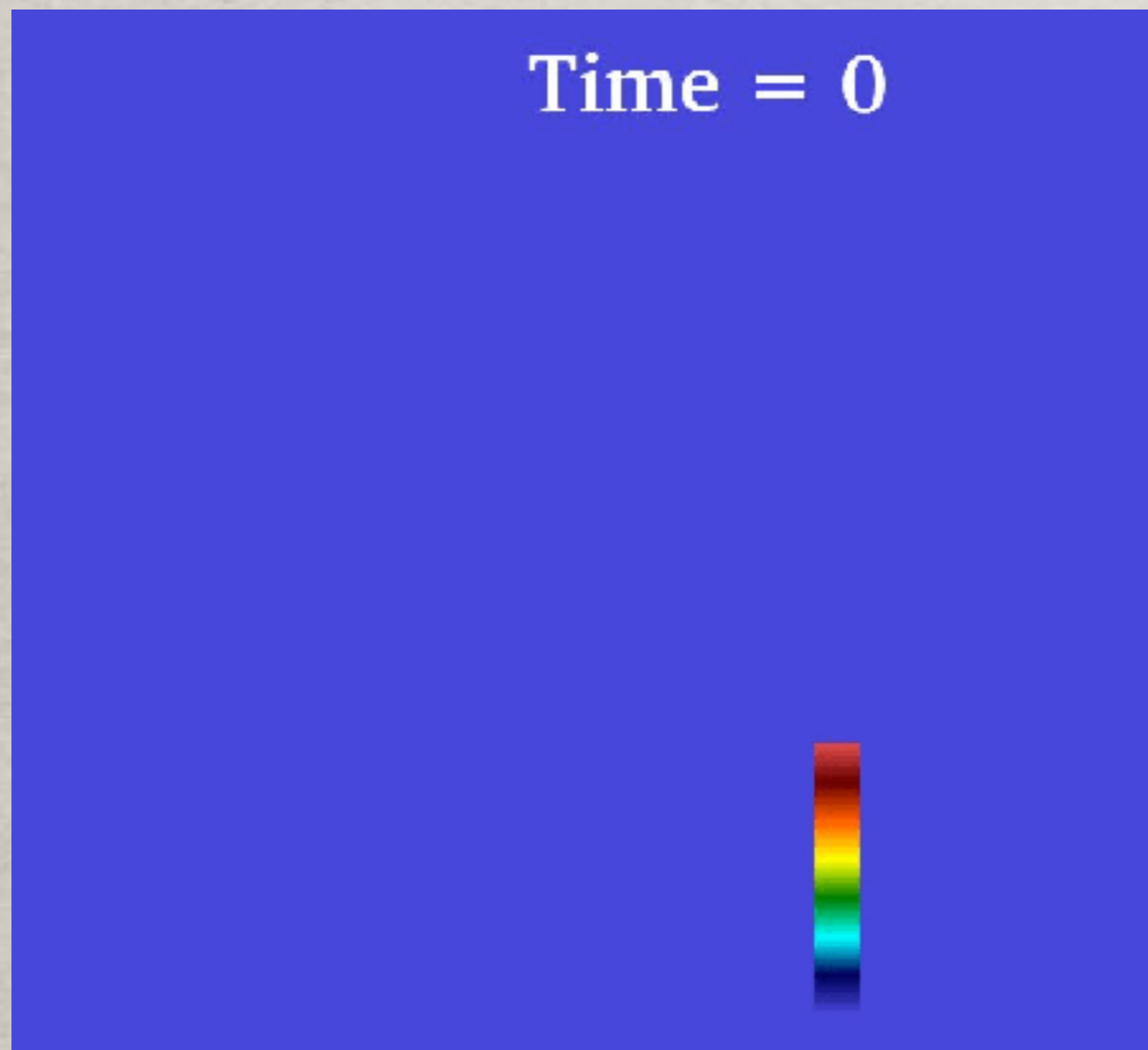
Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Evidence 3: - dynamics (formation scenario)

see e.g. Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101

Q3) what happens if we evolve a dilute cloud of spherical Proca field?



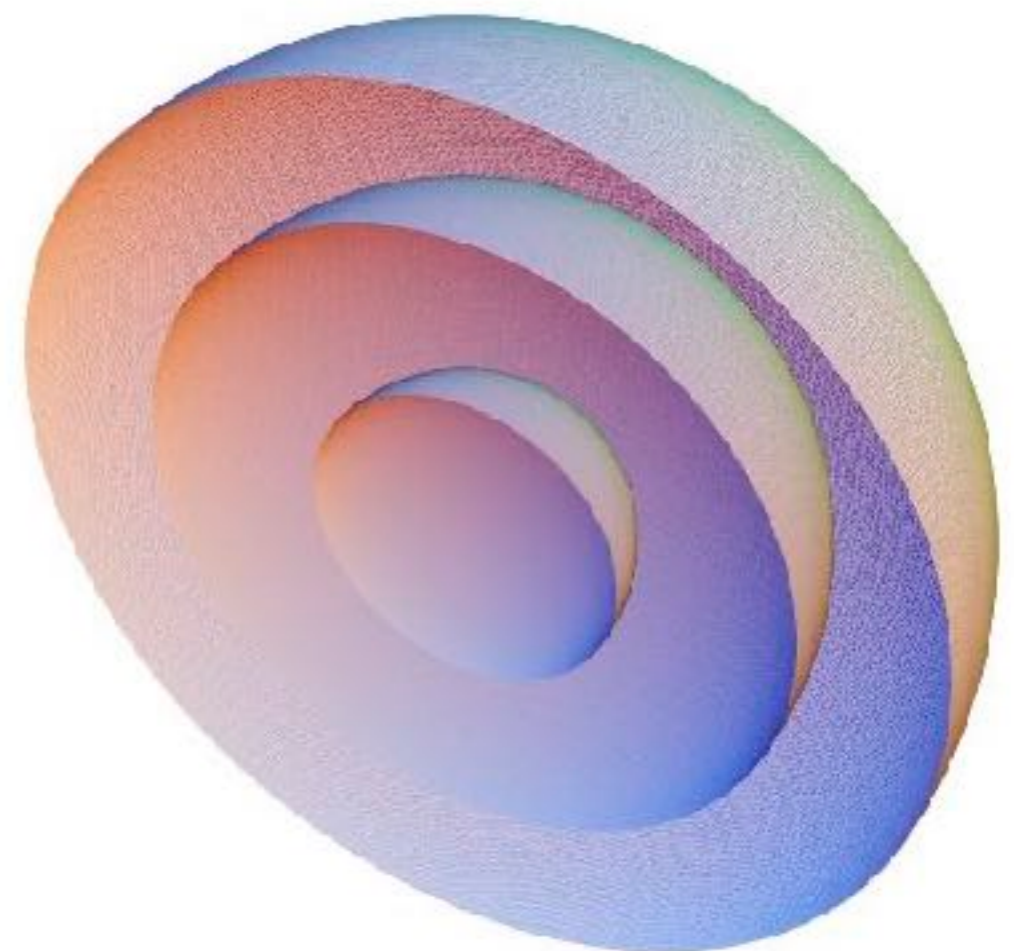
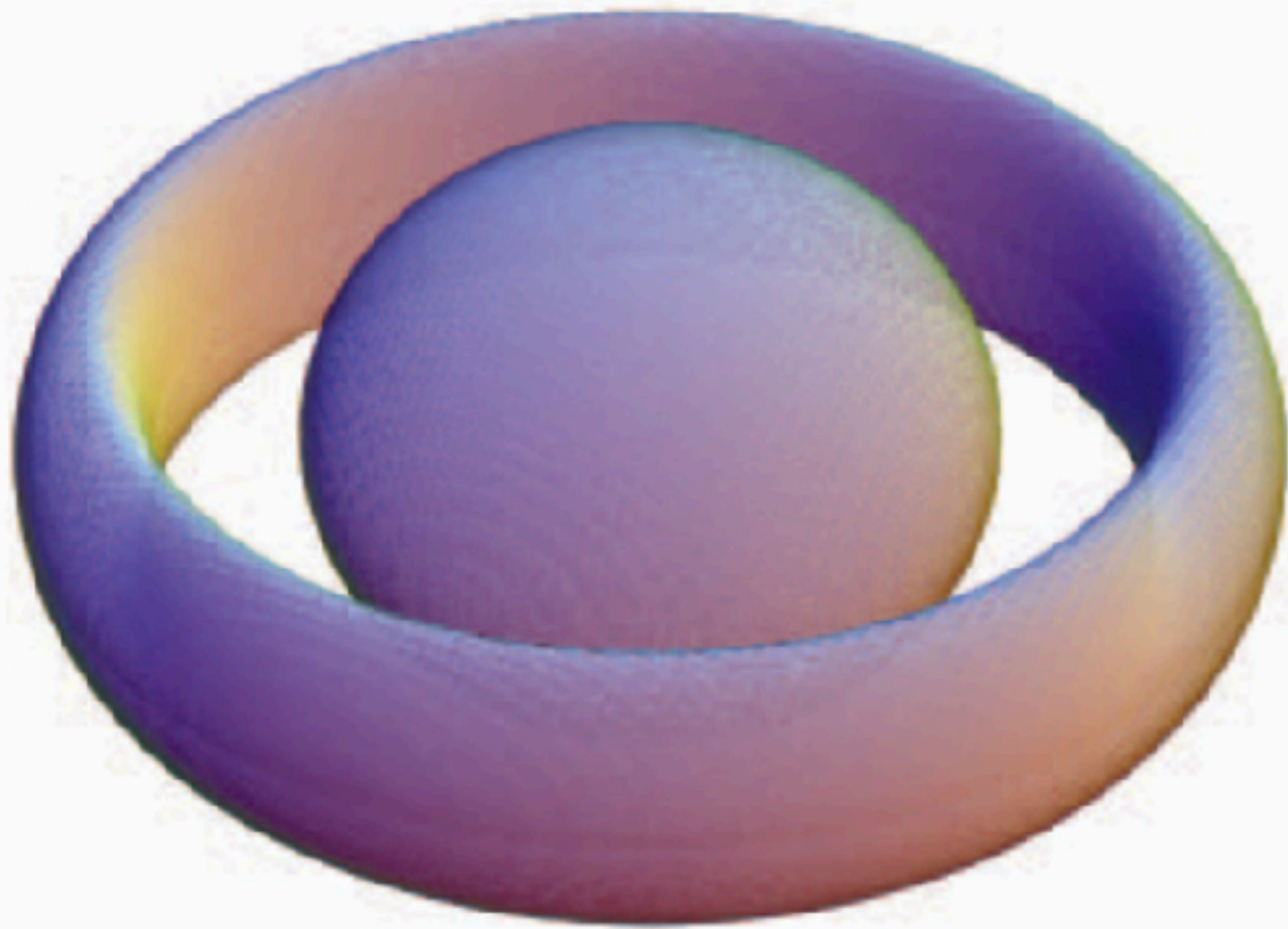
Spherical mini-PSs are unstable against a **non-spherical** perturbation

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

Comments:

- The prolateness (rather than spherical symmetry) of the ground state gives an example of a *static*, strong gravity system (which can reach a compactness comparable to that of black holes) that is not spherical;
- The instability of spherical Proca stars was missed in previous works because it was tacitly assumed that perturbative spherical stability was enough, and NR simulations were either too short or (inadvertently) imposed symmetries quenching/mitigating the instability;
- There are other interesting systems where a spherical configuration decays into a non-spherical one (e.g. a charged liquid drop).

Impact for rotating Proca stars?



First rotating Proca stars reported

Brito, Cardoso, CH and Radu, PLB 752 (2016) 291

CH, Radu and Rúnarsson, CQG 33 (2016) 154001

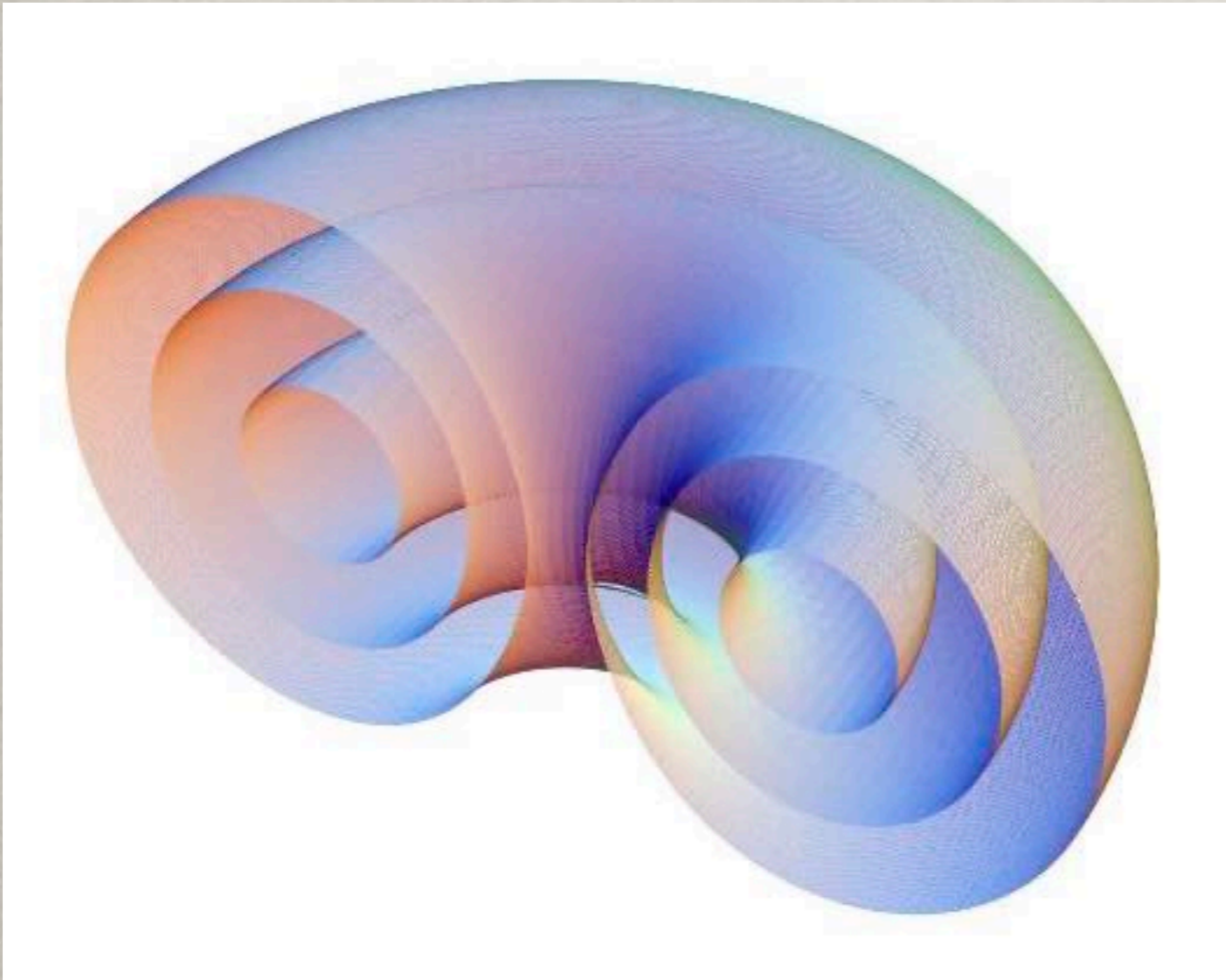
Rotating Proca stars without nodes

CH and Radu, PRL 119 (2017) 261101

CH, Perapechka, Radu and Shnir, PLB 797 (2019) 134845

In fact, these are known to be dynamically more robust
than spinning (scalar) boson stars

Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101



Rotating (scalar) boson stars

F. E. Schunck and E. W. Mielke, PLA 249 (1998) 389

S. Yoshida and Y. Eriguchi, PRD 56 (1997) 762



Rotating Proca stars without nodes

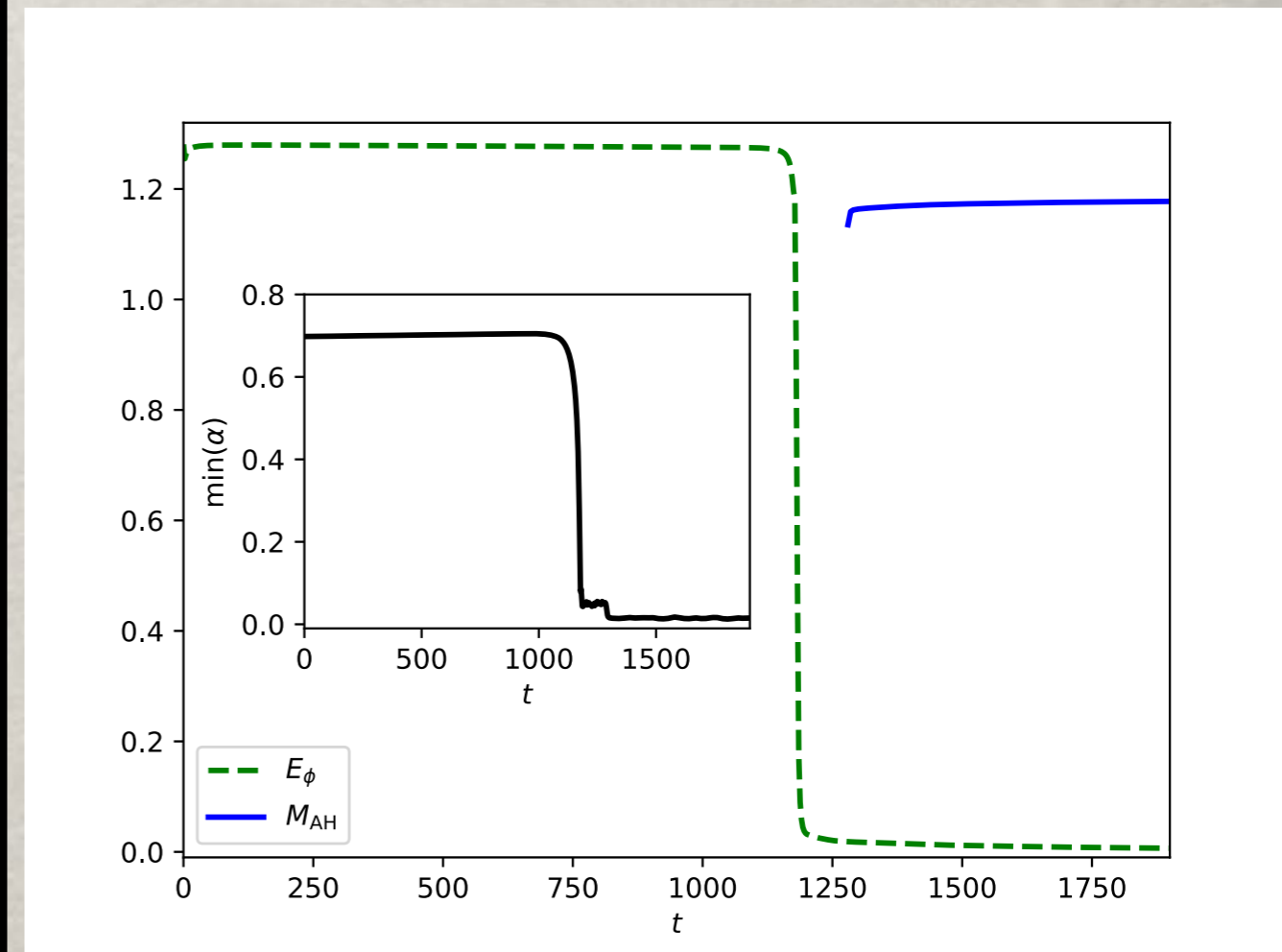
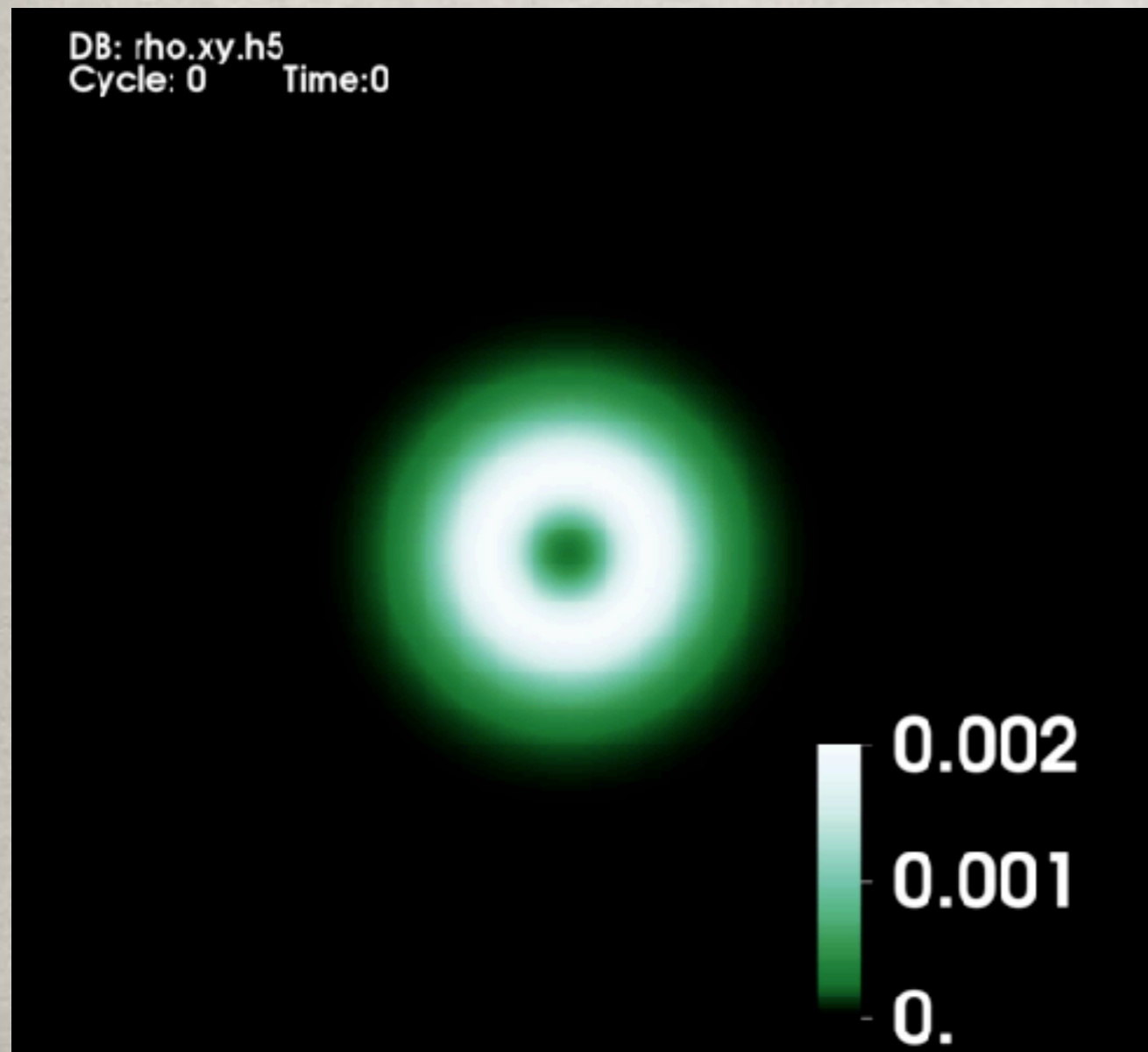
CH and Radu, PRL 119 (2017) 261101

CH, Perapechka, Radu and Shnir, PLB 797 (2019) 134845

Spinning scalar boson stars have a non-axisymmetric instability

Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101

<http://gravitation.web.ua.pt/node/1740>

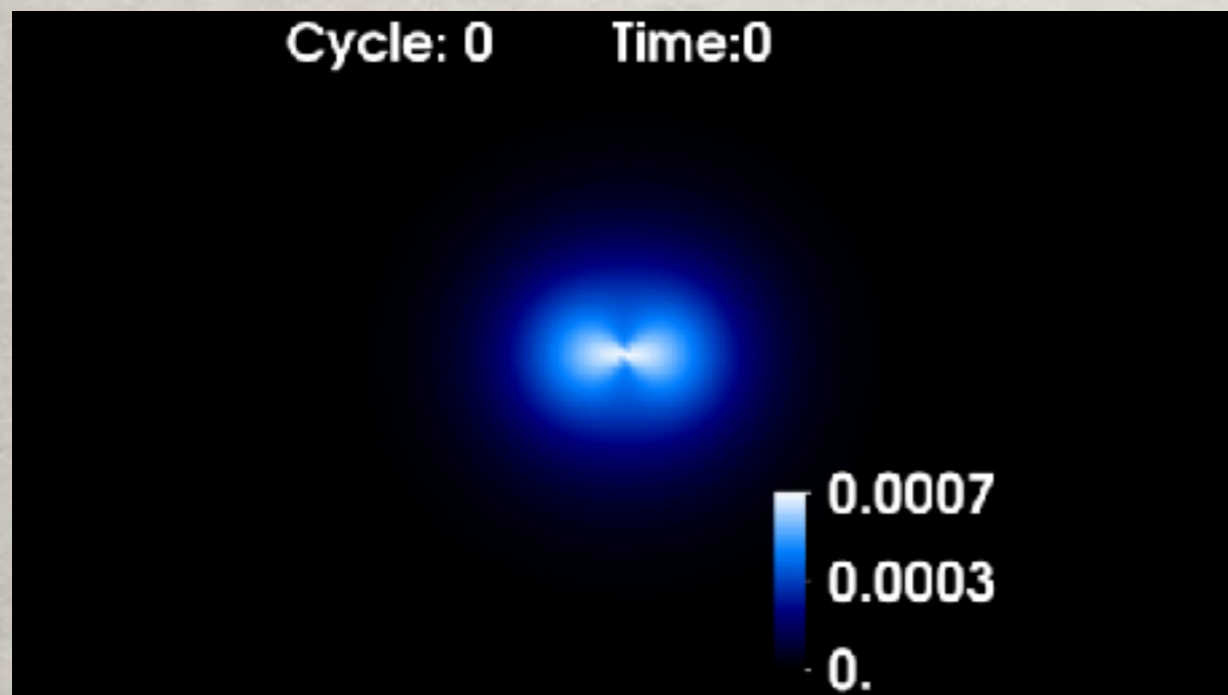


Spinning Proca stars do not exhibit such instability.

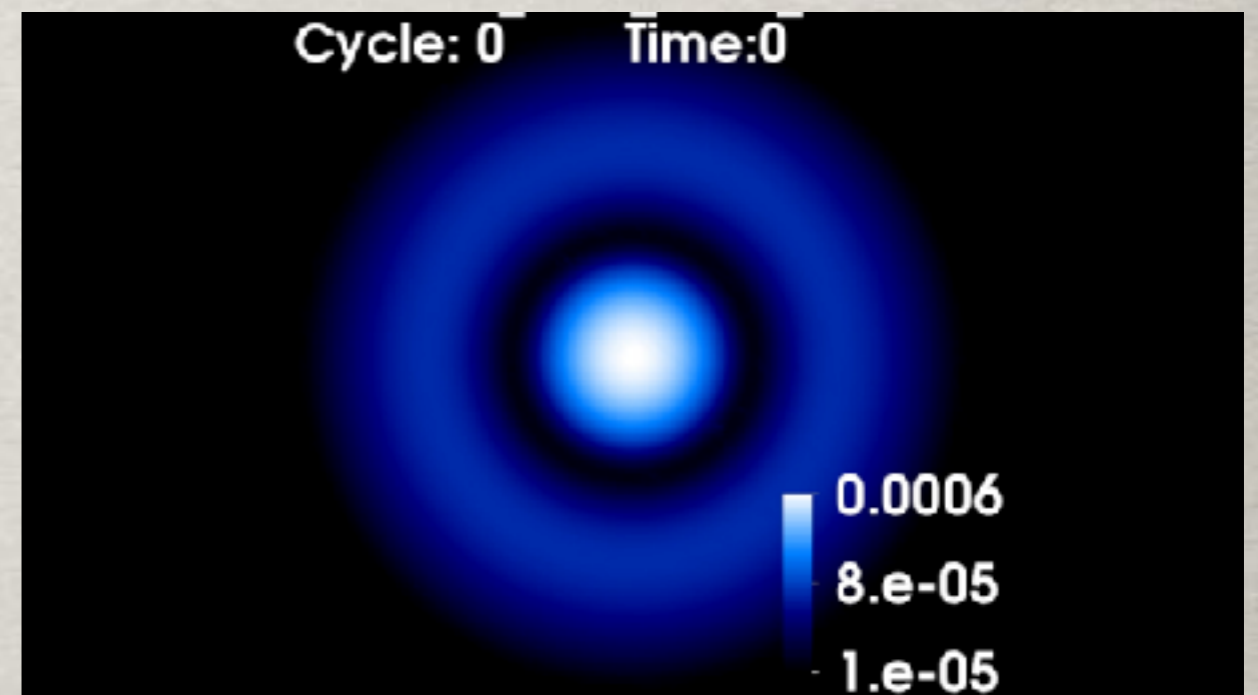
Sanchis-Gual, Di Giovanni, Zilhão, CH, Cerda-Duran, Font and Radu, PRL 123 (2019) 221101

<http://gravitation.web.ua.pt/node/1740>

Evolution of a perturbed
spinning Proca star



Evolution of an excited
spinning Proca star



Thus, spinning Proca stars are dynamically more robust in these simplest models.

But in models with self-interactions, the spinning scalar stars instability can be mitigated.

Di Giovanni, Sanchis-Gual, Cerdan-Duran, Zilhão, CH, Font and Radu, PRD 102 (2020) 124009;

Siemonson and East, PRD 103 (2021) 044022

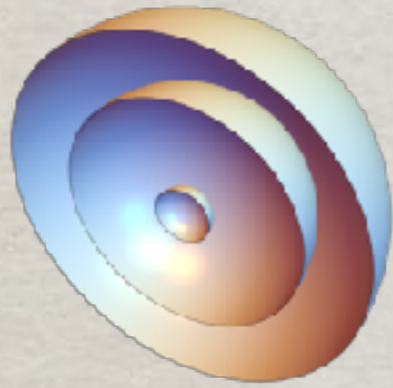
A surprising (dynamically) different picture:

Costa, CH, Radu, Sanchis-Gual and Santos, 2311.14800

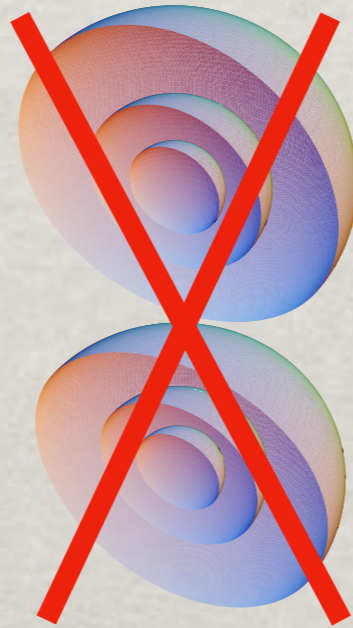
Static:

Spinning:

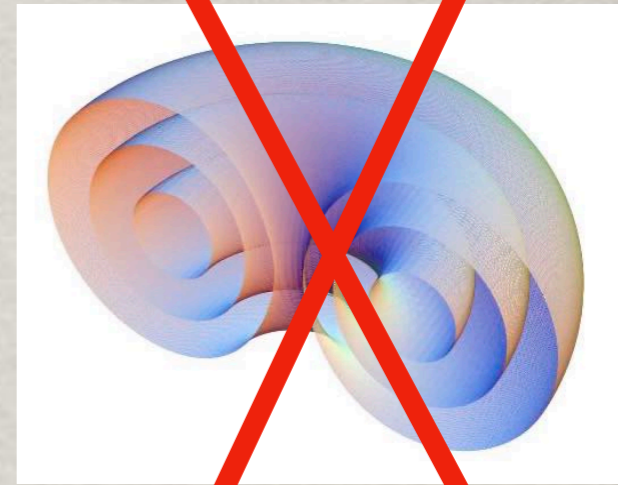
Scalar



Monopole

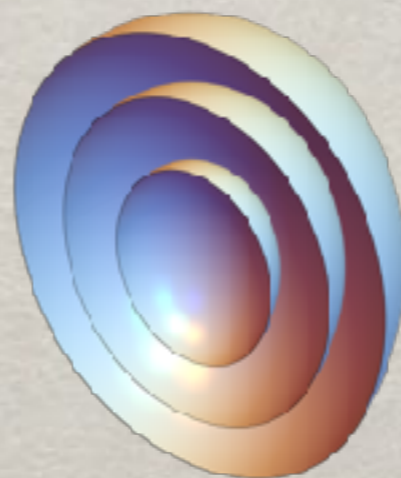


Dipole

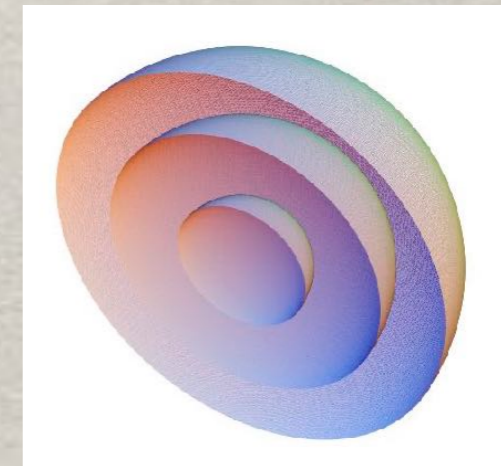


Toroidal

Vector



Spheroidal

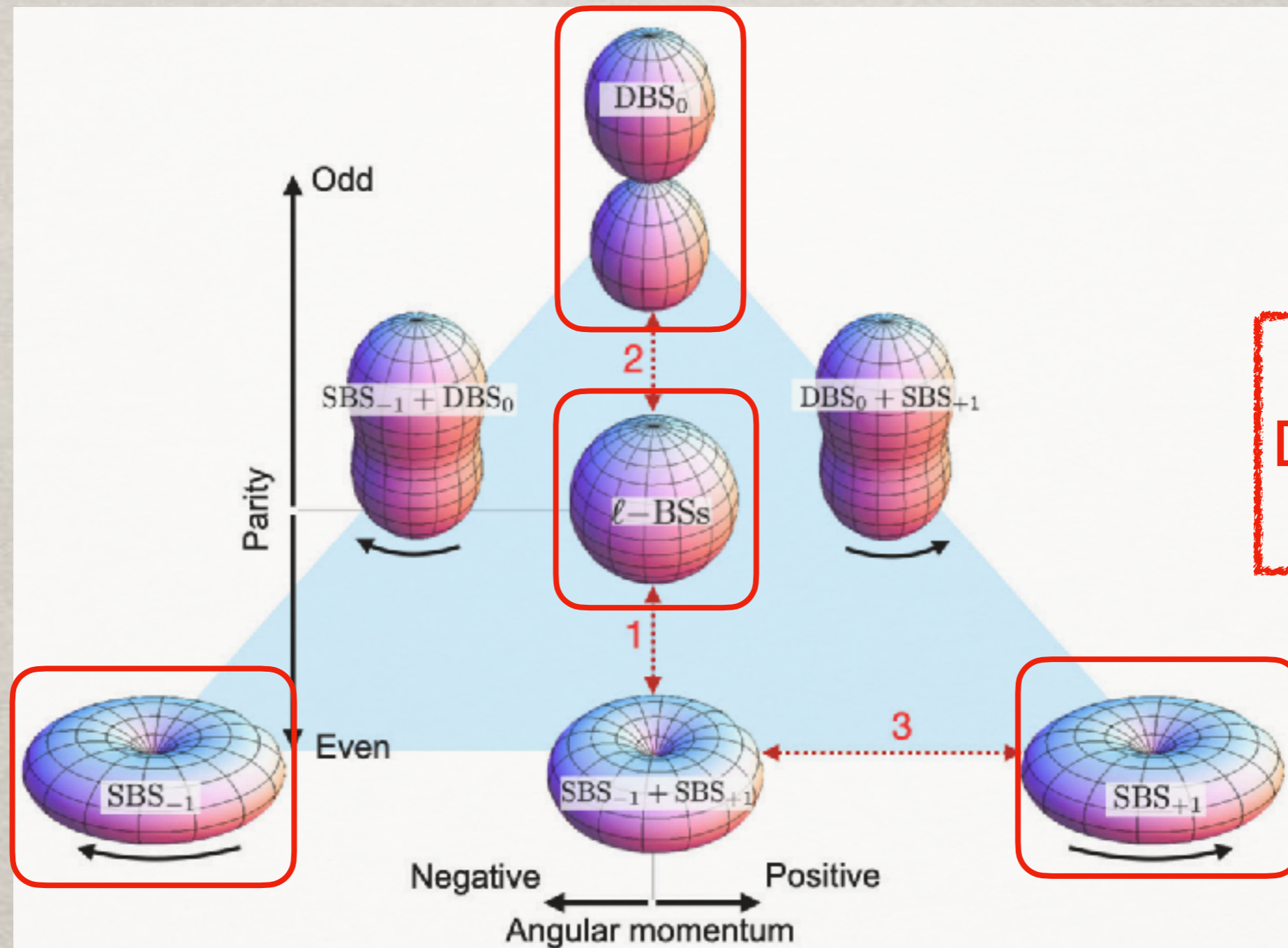


Composite stars (multi-state, multi-frequency):

Matos, Urena-Lopez, GRG 39 (2007) 1279; Bernal, Barranco, Alic, Palenzuela, PRD 81 (2010) 044031;

Urena-Lopez and Bernal, PRD 82 (2010) 123535; Alcubierre, Barranco, Bernal, Degollado, Diez-Tejedor, Megevand, Nunez, Sarbach, CQG 35, 19LT01 (2018); Di Giovanni, Fakhry, Sanchis-Gual, Degollado, and Font, PRD 102 (2020) 084063; F. S. Guzmán and L. A.

Ureña López, PRD 101 (2020) 081302(R); F. S. Guzmán, Astron. Nachr. 342 (2021) 398



J. C. Degollado's talk

FIG. 1. $\ell = 1$ BSs family.

II) Some phenomenology (and the imitation game)

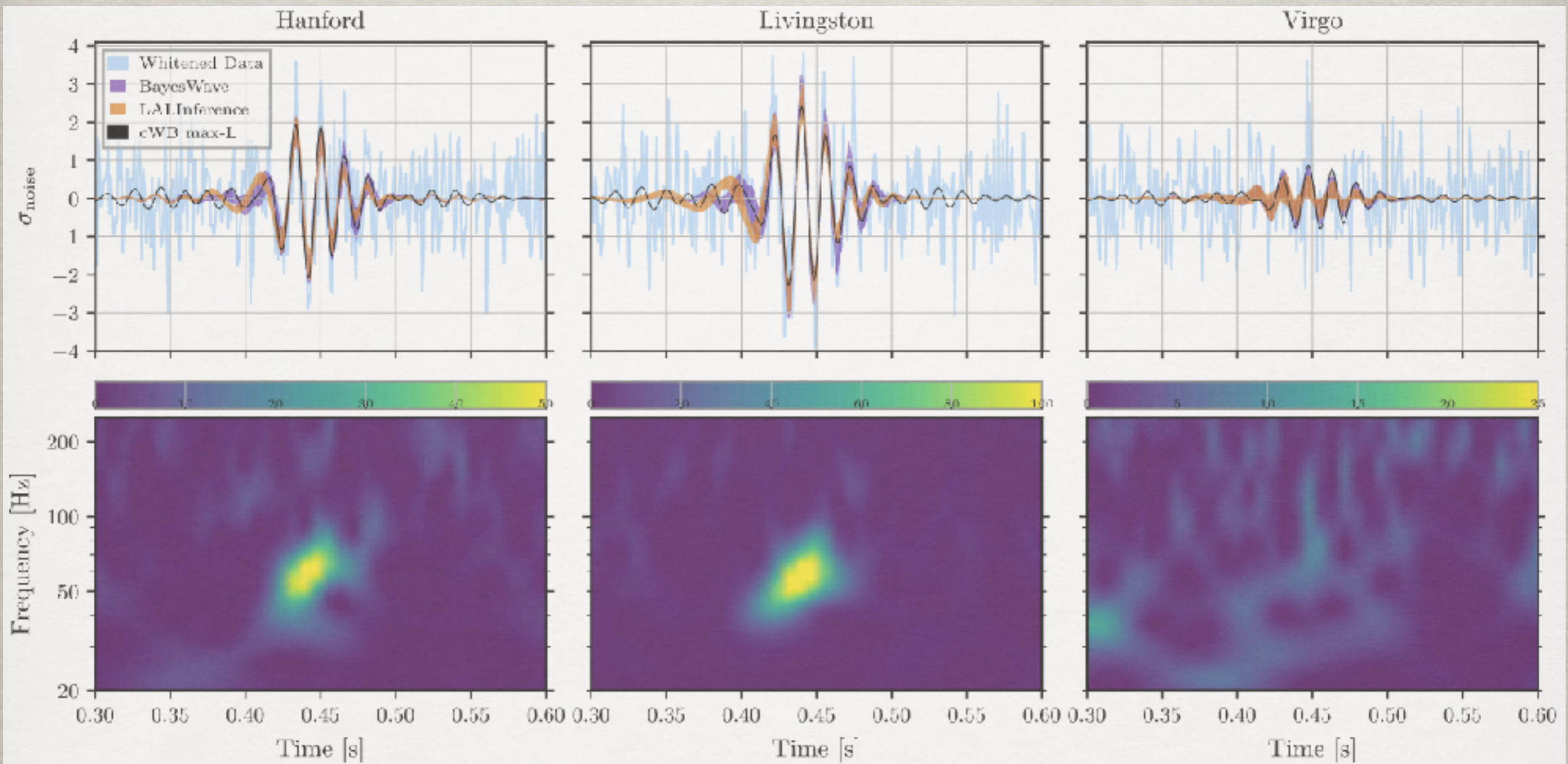
The imitation game

a) Mimicking a gravitational wave event

A particular event from the O3 run





<https://gracedb.ligo.org/superevents/public/O3/>

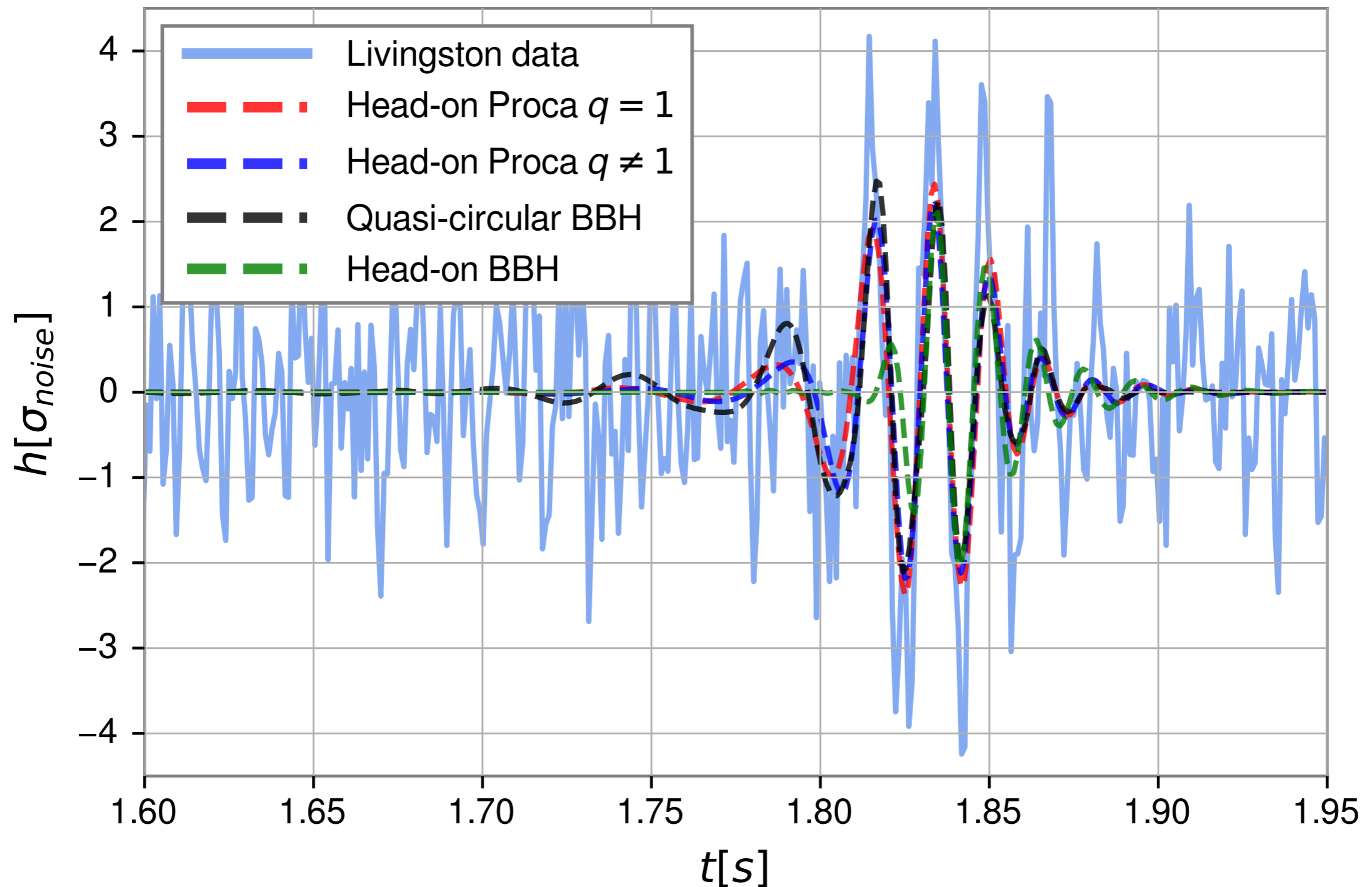
GW190521 PRL 125 (2020) 10, ApJ Lett. 900 (2020) L13



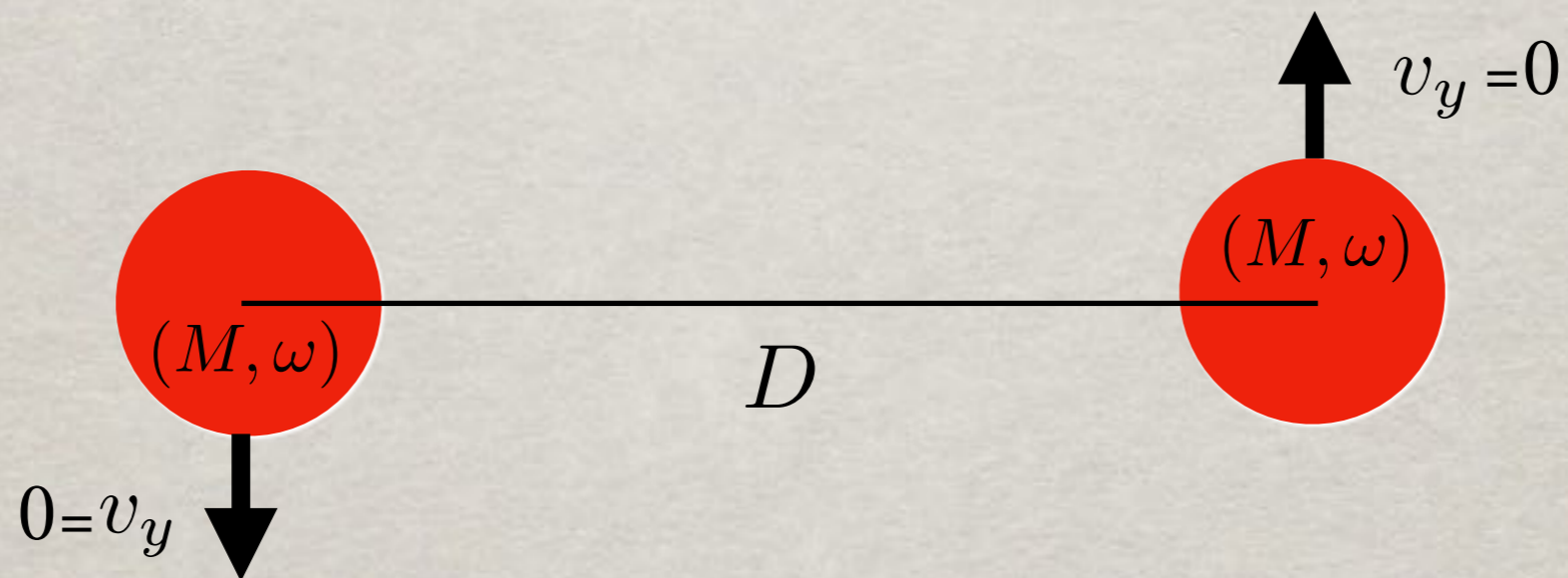
- Two most massive progenitors: $85_{-14}^{+21}M_{\odot}$, $66_{-18}^{+17}M_{\odot}$
- At least one in the pair instability supernova gap. Formation?
- Very short - no inspiral
- Final BH can be considered of intermediate mass: $142_{-16}^{+28}M_{\odot}$

GW190521 as a Merger of Proca Stars: A Potential New Vector Boson of 8.7×10^{-13} eV

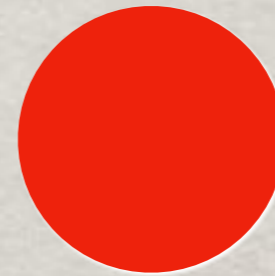
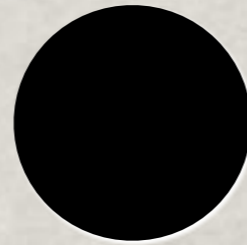
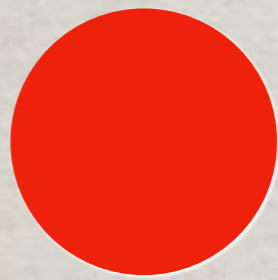
Juan Calderón Bustillo ^{1,2,3,4,*} Nicolas Sanchis-Gual ^{5,6,†} Alejandro Torres-Forné,^{7,8,9} José A. Font ^{8,9} Avi Vajpeyi,^{3,4}
Rory Smith ^{3,4} Carlos Herdeiro ⁶ Eugen Radu,⁶ and Samson H. W. Leong ²



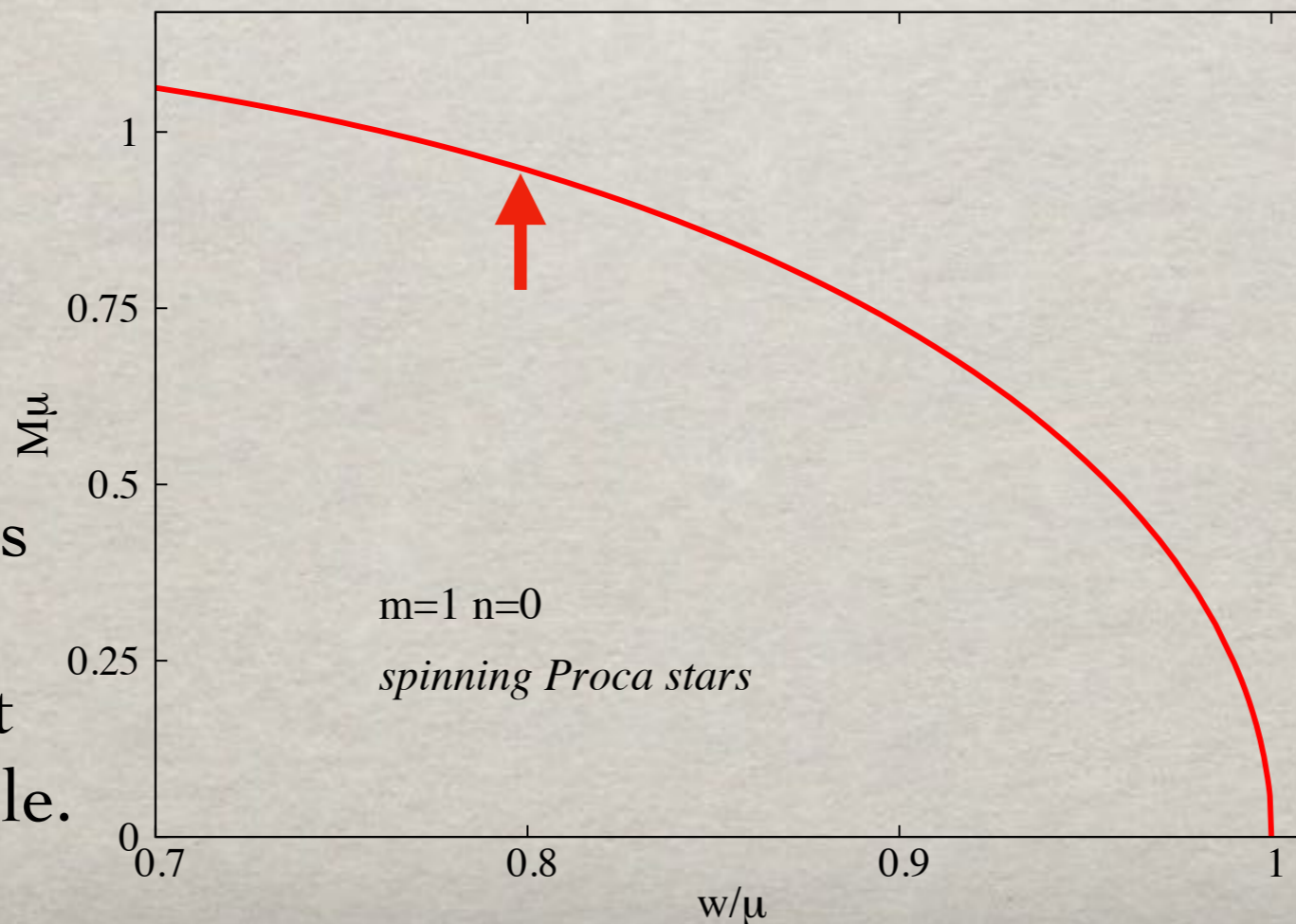
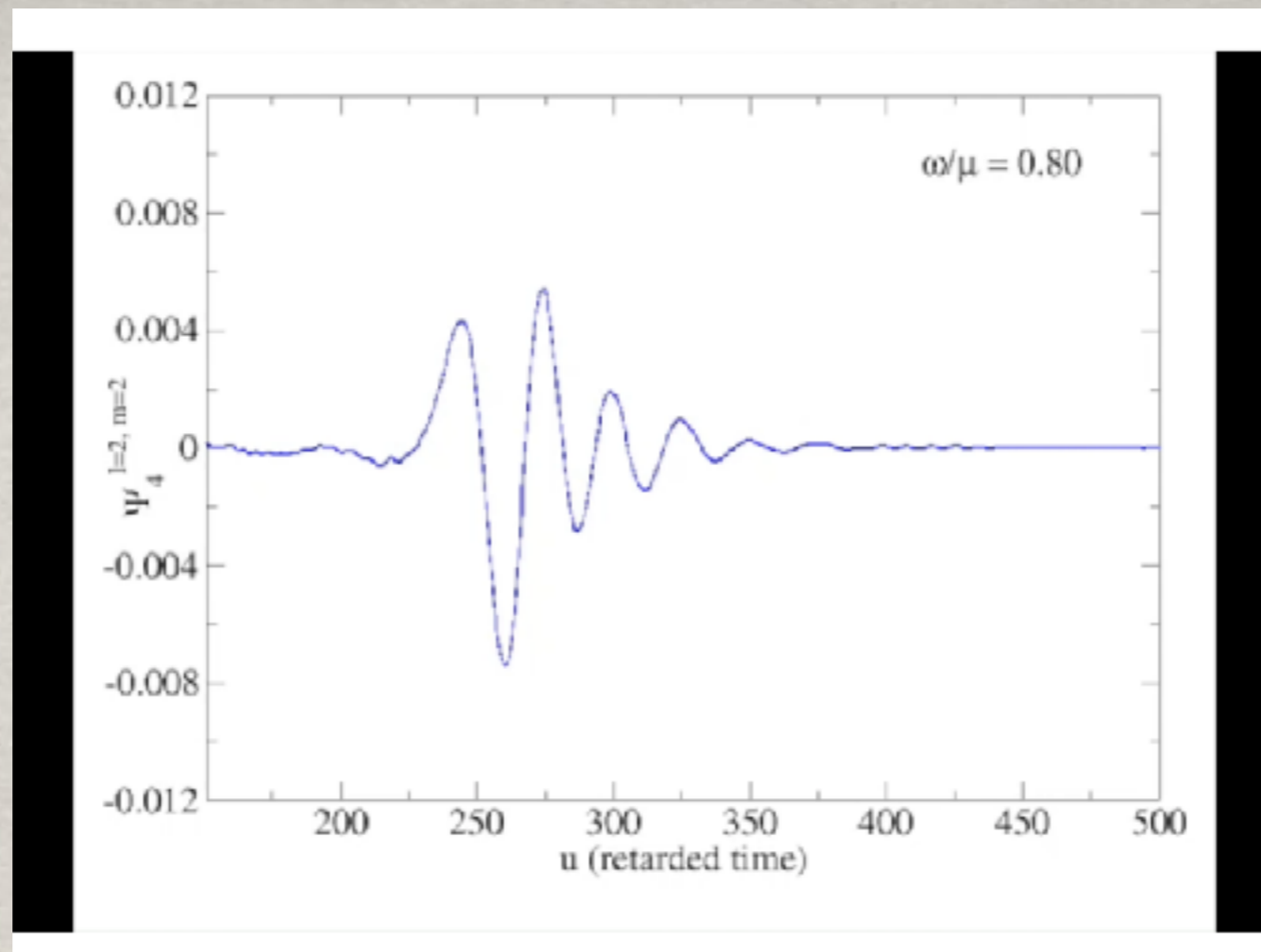
Mergers of spinning vector boson stars



Mergers of spinning vector boson stars



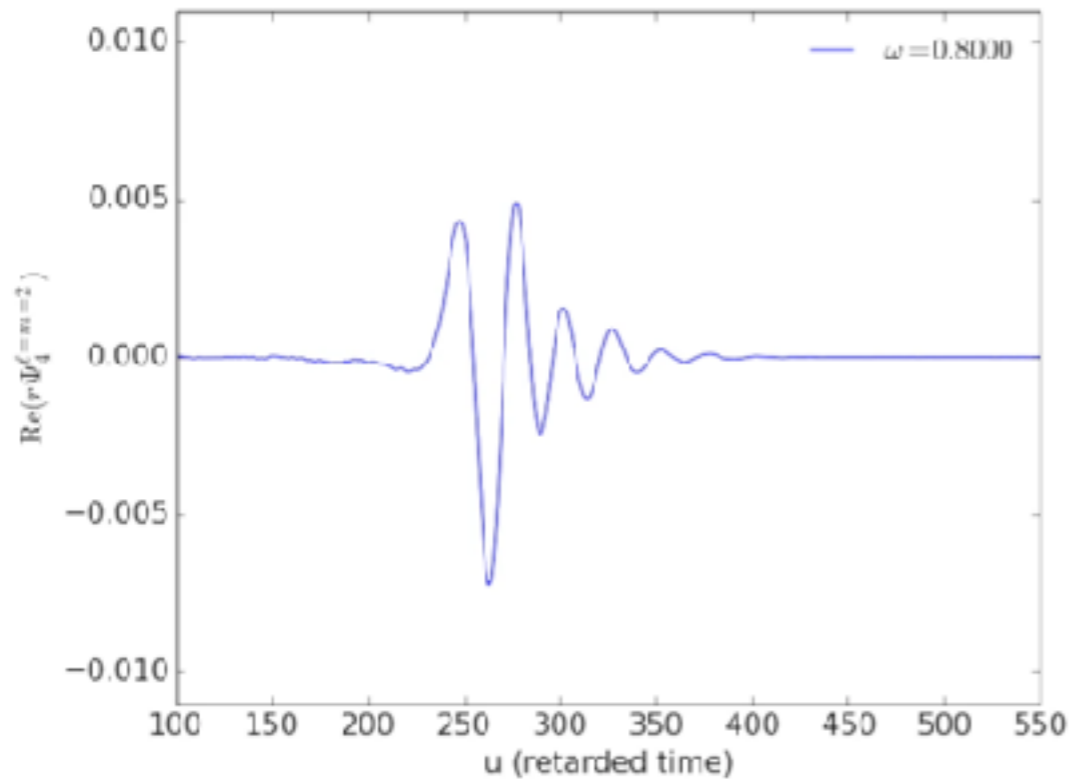
$(M_{\text{BH}}, J_{\text{BH}})$



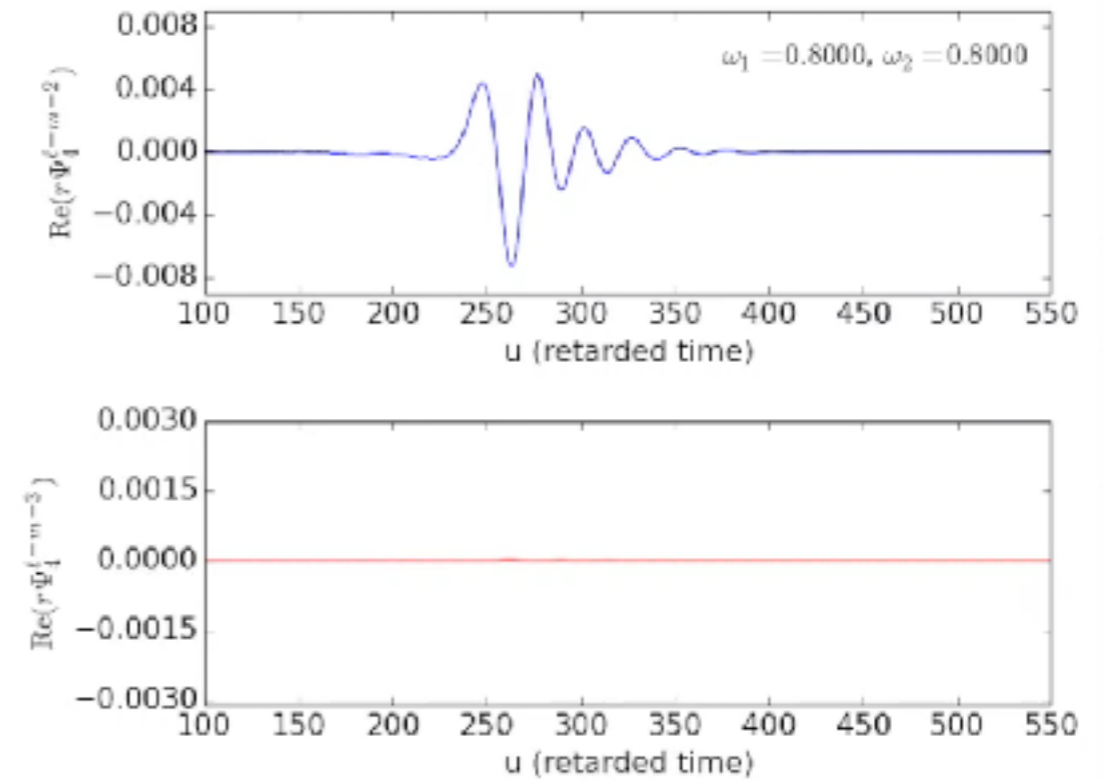
For frequencies
 too high
 the final object
 is not a black hole.

These examples are
 for equal masses, but
 we have also
 performed unequal
 mass collisions.

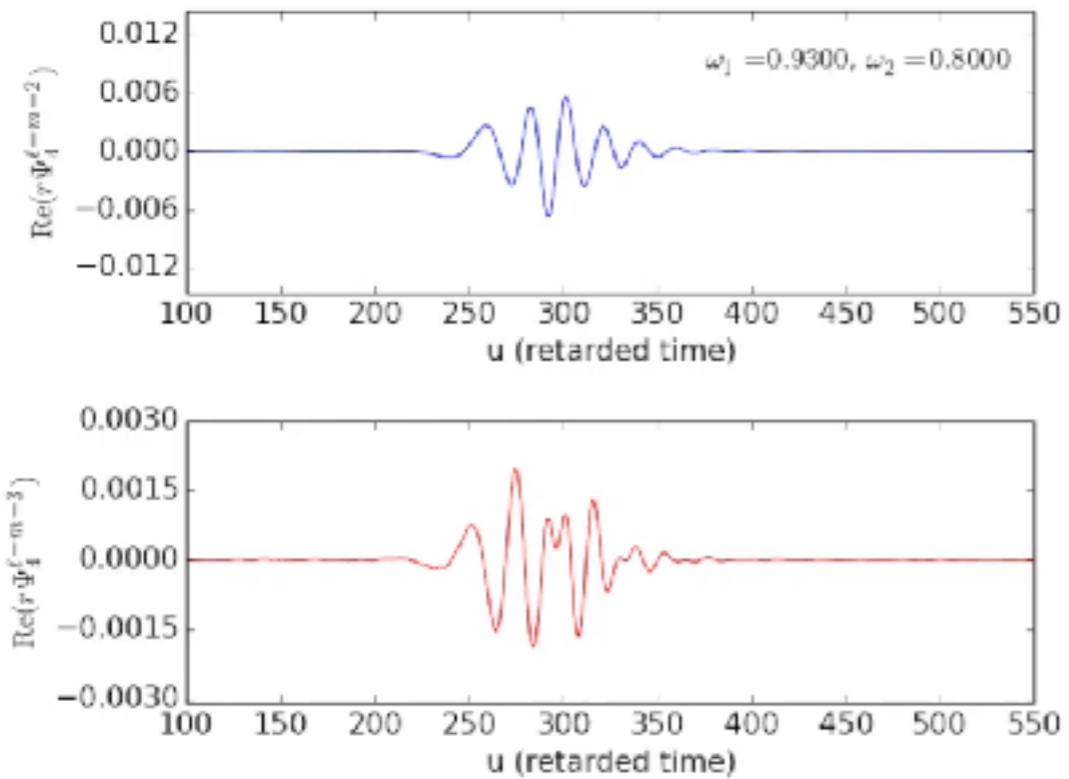
equal mass



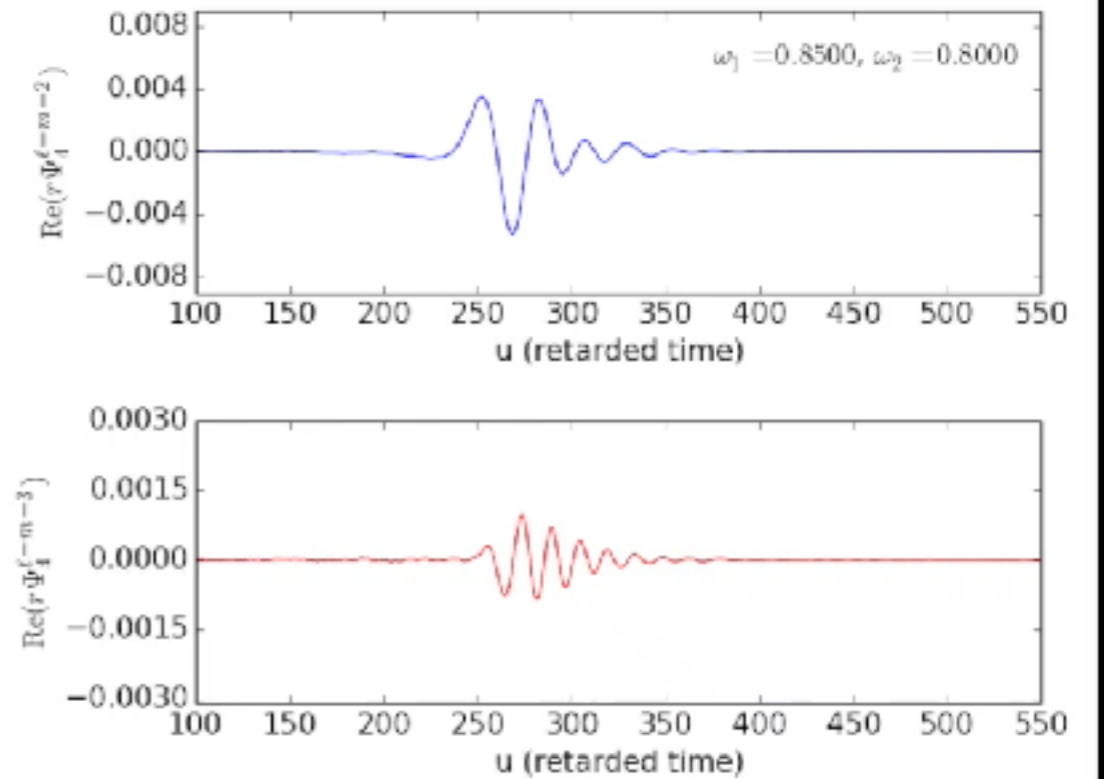
unequal mass



unequal mass



unequal mass

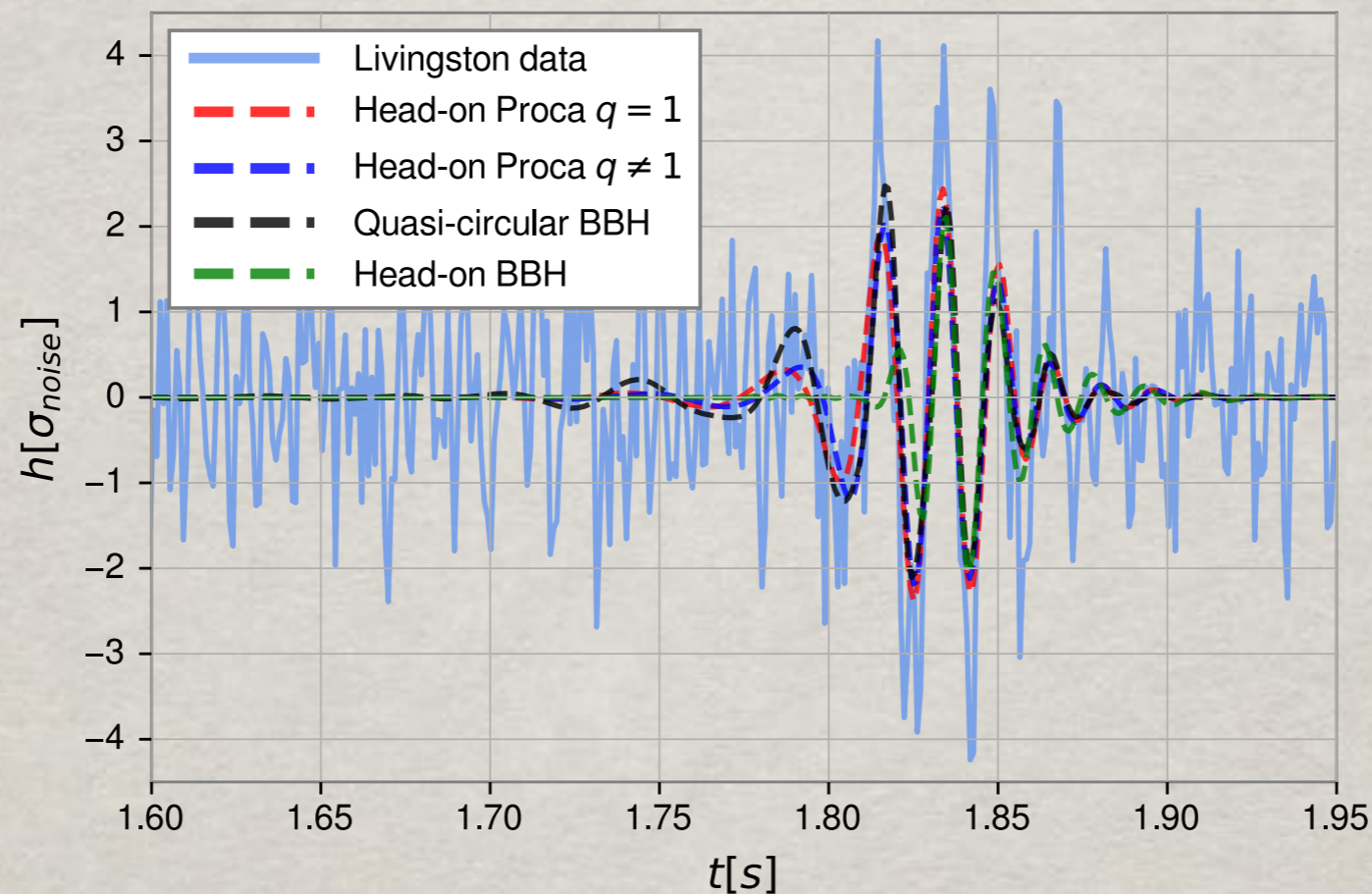


Building a catalogue of Proca star waveforms

(over 750 waveforms from NR simulations so far) [Sanchis-Gual+ 2208.11717](#)

Statistical Preference:

Bustillo et. al, PRL 126 (2021) 081181



Waveform model	$\log \mathcal{B}$	$\log \mathcal{L}_{\max}$
Quasi-circular Binary Black Hole	80.1	105.2
Head-on Equal-mass Proca Stars	80.9	106.7
Head-on Unequal-mass Proca Stars	82.0	106.5
Head-on Binary Black Hole	75.9	103.2

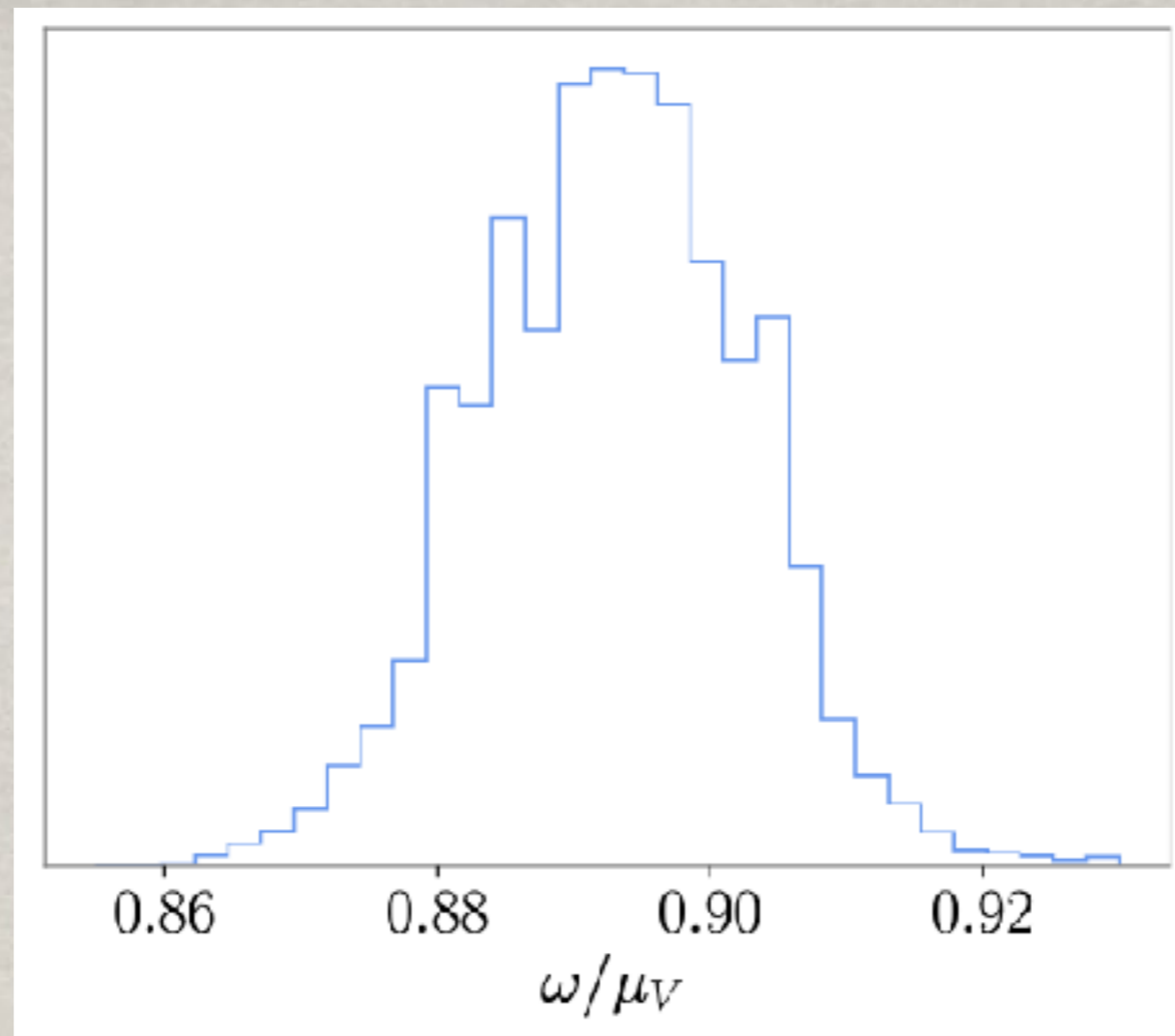
Prior:

Uniform in co-moving volume

Waveform Model	$\log \mathcal{B}$	$\log \mathcal{L}_{Max}$
Quasi-circular Binary Black Hole	80.1	105.2
Head-on Equal-mass Proca Stars	83.5	106.7
Head-on Unequal-mass Proca Stars	84.3	106.5
Head-on Binary Black Hole	78.0	103.2

Prior:

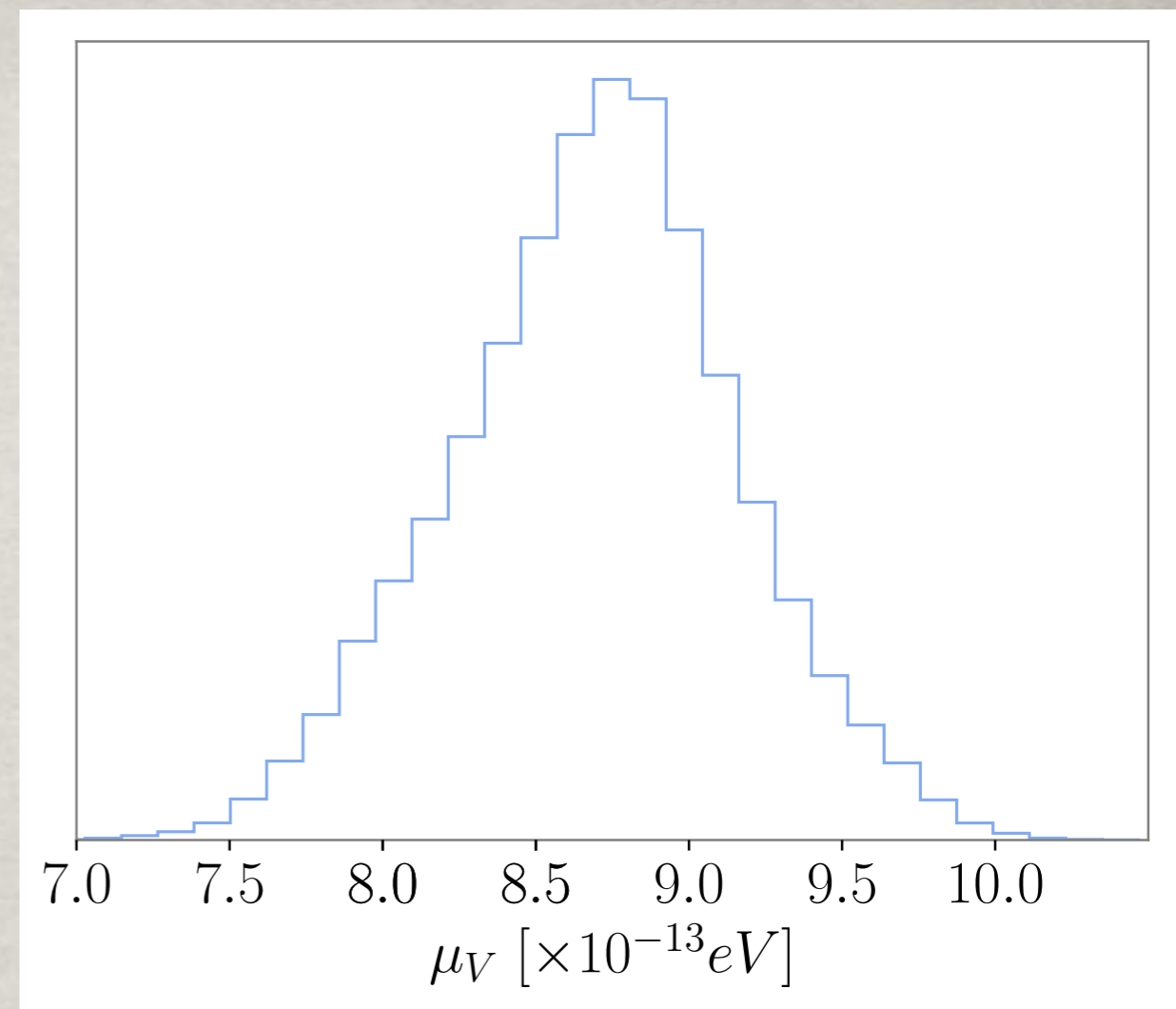
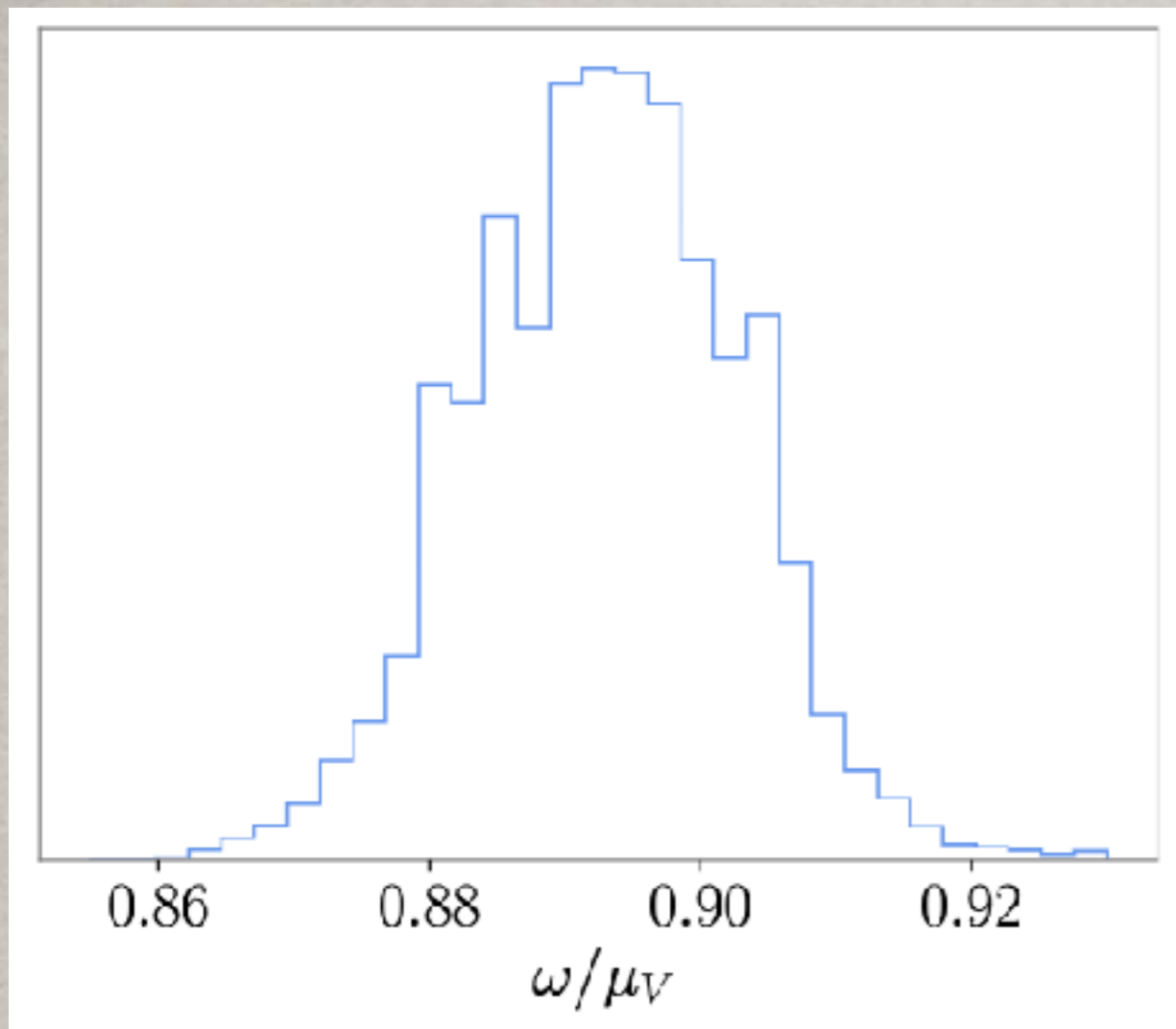
Uniform in distance



$$\omega/\mu_V = 0.893^{+0.015}_{-0.015}$$

Determines $M\mu_V$

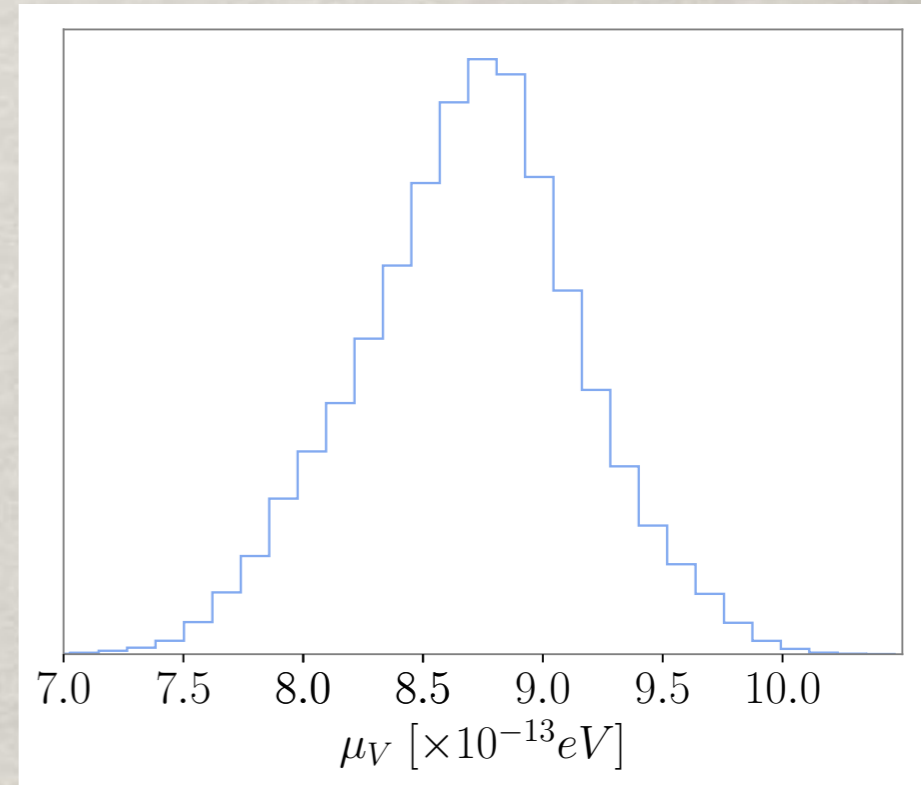
Identifying the mass of each Proca star as half of the mass of the final black hole determines the mass of the ultralight boson.



Thus we get a distribution for the mass of the ultralight boson.

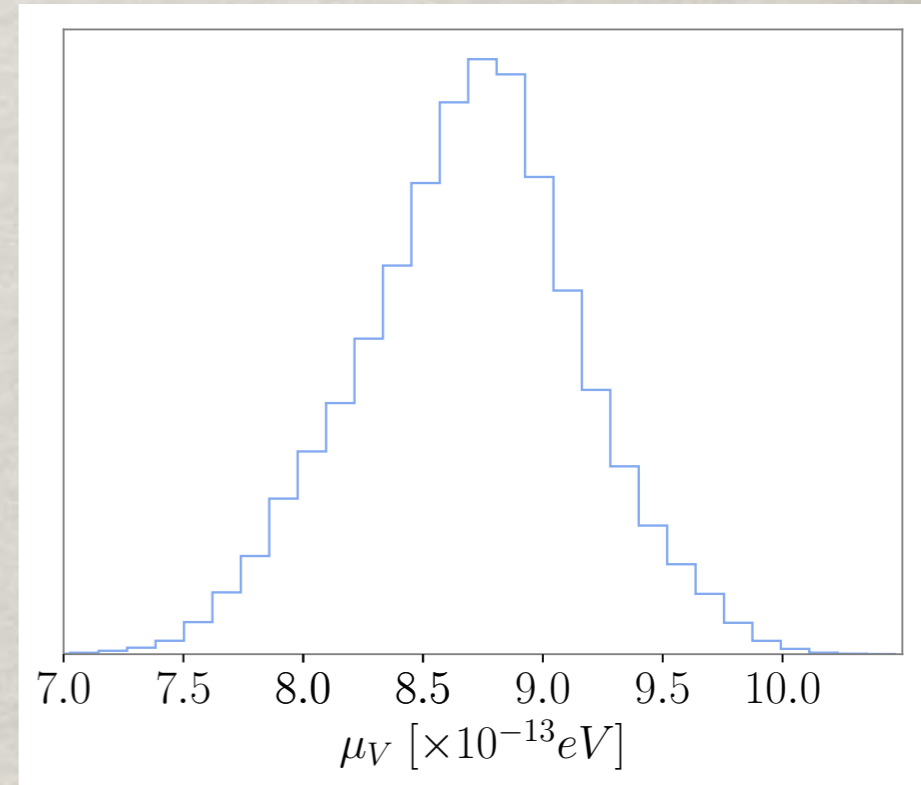
Gravitating scalar/vector solitons: bosonic stars

Parameter	$q = 1$ model	$q \neq 1$ model
Primary mass	$115_{-8}^{+7} M_{\odot}$	$115_{-8}^{+7} M_{\odot}$
Secondary mass	$115_{-8}^{+7} M_{\odot}$	$111_{-15}^{+7} M_{\odot}$
Total / Final mass	$231_{-17}^{+13} M_{\odot}$	$228_{-15}^{+17} M_{\odot}$
Final spin	$0.75_{-0.04}^{+0.08}$	$0.75_{-0.04}^{+0.08}$
Inclination $\pi/2 - \iota - \pi/2 $	$0.83_{-0.47}^{+0.23}$ rad	$0.58_{-0.39}^{+0.40}$ rad
Azimuth	$0.65_{-0.54}^{+0.86}$ rad	$0.78_{-1.20}^{+1.23}$ rad
Luminosity distance	571_{-181}^{+348} Mpc	700_{-279}^{+292} Mpc
Redshift	$0.12_{-0.04}^{+0.05}$	$0.14_{-0.05}^{+0.06}$
Total / Final redshifted mass	$258_{-9}^{+9} M_{\odot}$	$261_{-11}^{+10} M_{\odot}$
Bosonic field frequency ω/μ_V	$0.893_{-0.015}^{+0.015}$	(*) $0.905_{-0.042}^{+0.012}$
Boson mass $\mu_V [\times 10^{-13}]$	$8.72_{-0.82}^{+0.73}$ eV	$8.59_{-0.57}^{+0.58}$ eV
Maximal boson star mass	$173_{-14}^{+19} M_{\odot}$	$175_{-11}^{+13} M_{\odot}$



Gravitating scalar/vector solitons: bosonic stars

Parameter	$q = 1$ model	$q \neq 1$ model
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Maximal boson star mass	$173_{-14}^{+19} M_{\odot}$	$175_{-11}^{+13} M_{\odot}$



$$M_{\text{max}} = 173_{-14}^{+19} M_{\odot}$$

No previous
GW signals
can be Proca star
mergers.

The imitation game

b) Mimicking a black hole shadow without light rings

P. Cunha's

H. Lima Junior's

S. Dolan's
talks

The edge of the shadow is determined by the

Fundamental Photon Orbits

Cunha, C.H., Radu, PRD 96 (2017) 024039

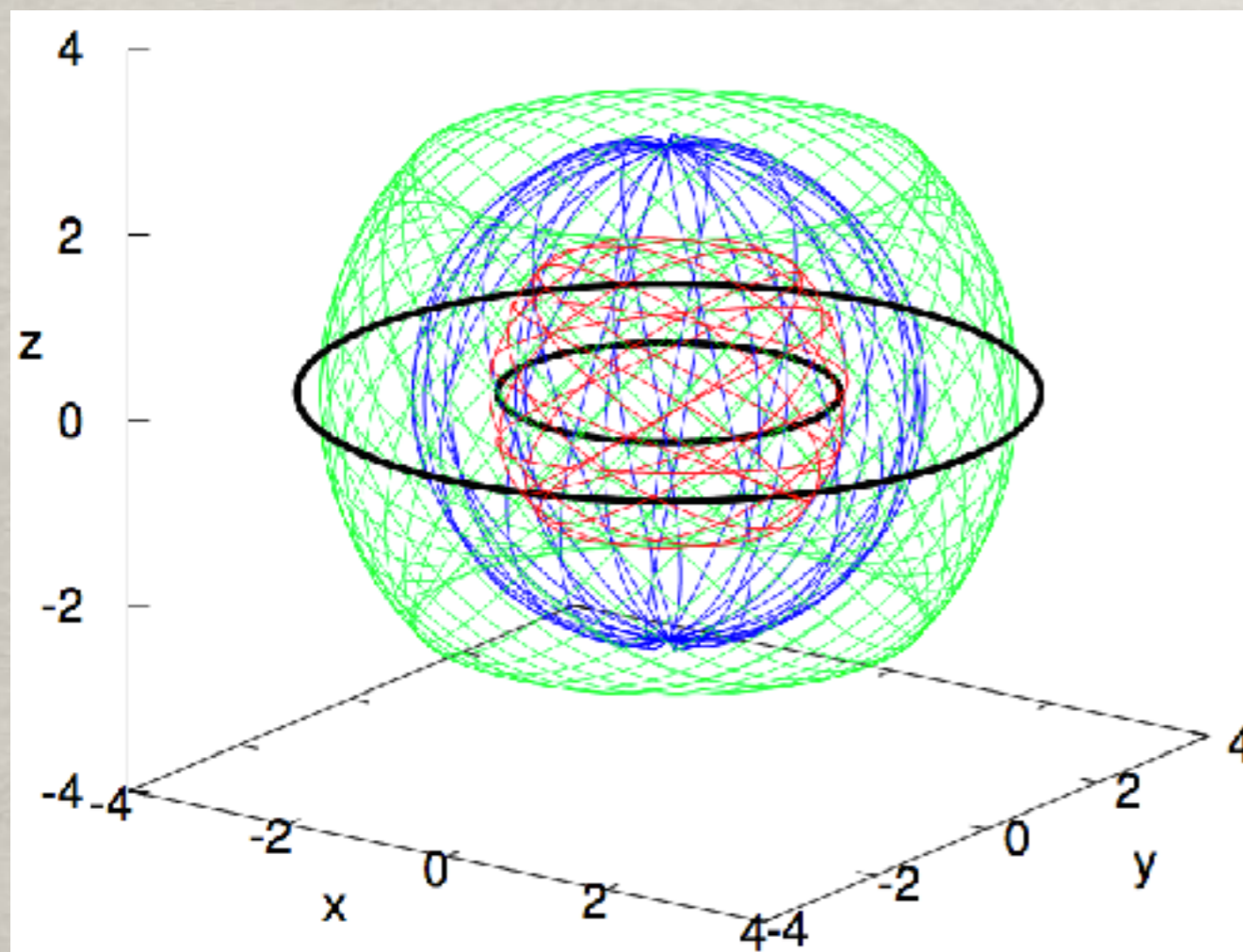
Called spherical orbits in Kerr case

Teo, GRG 35 (2003) 1909

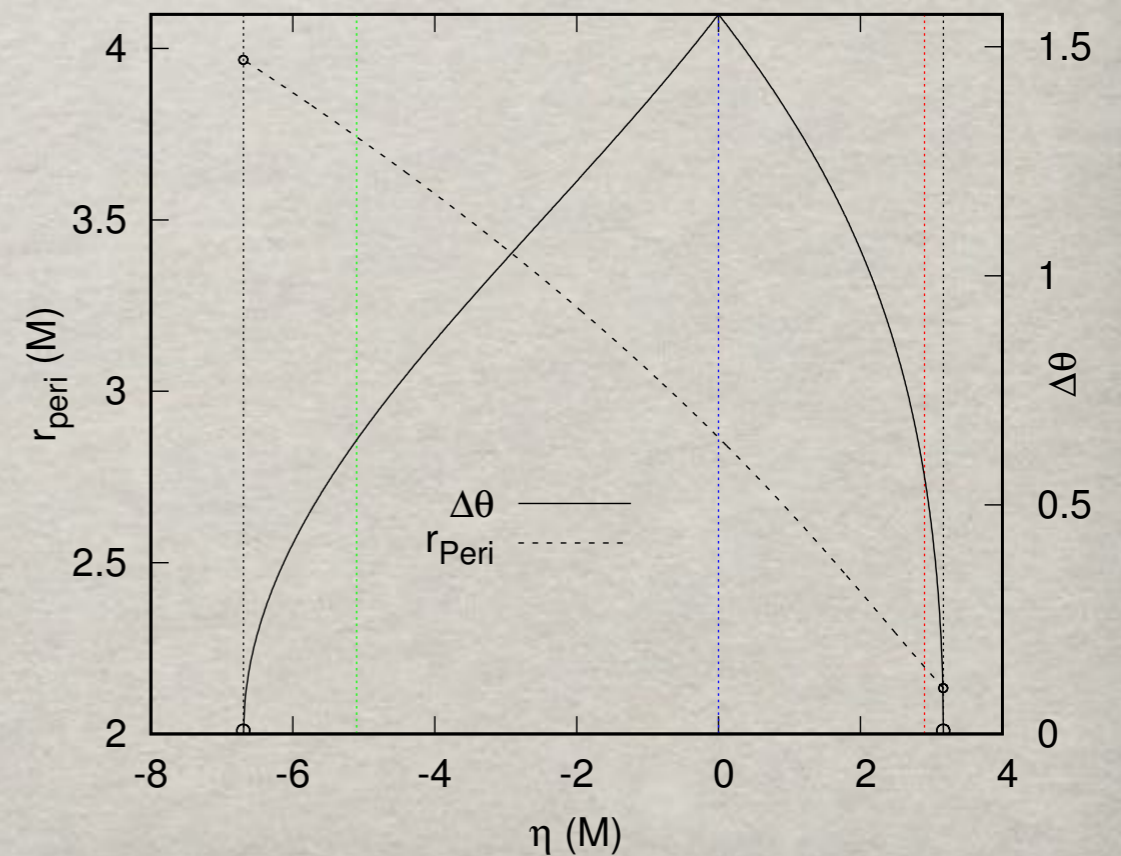
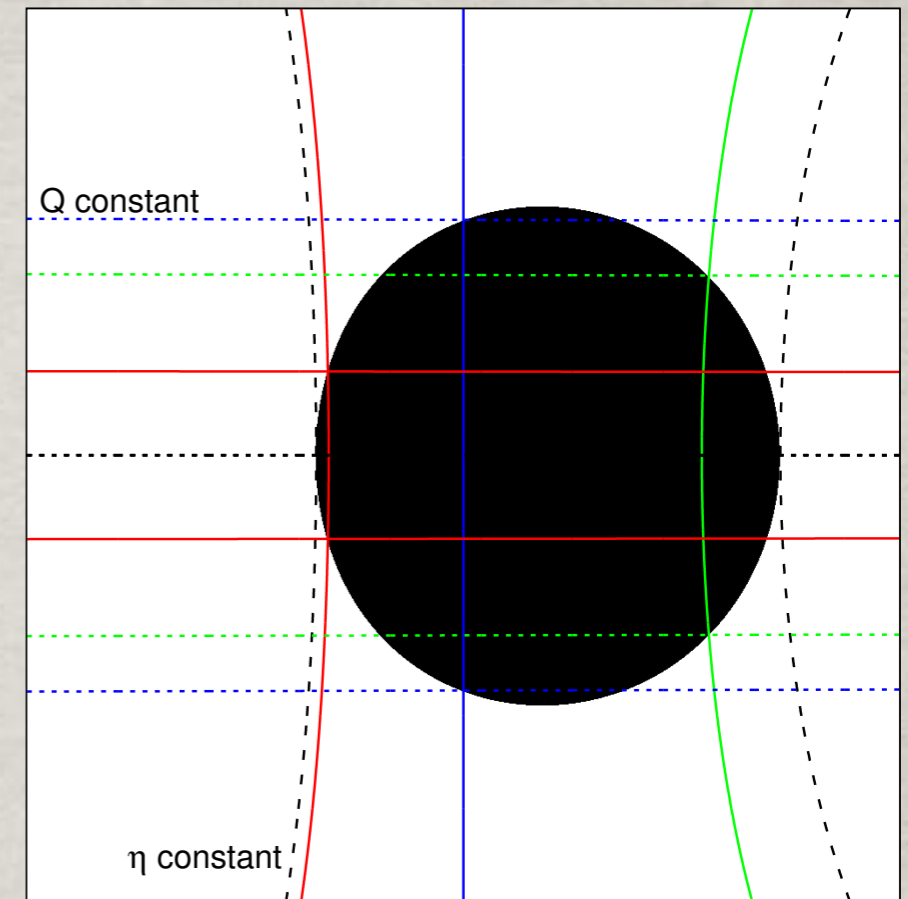
Relate to quasi-normal ringing

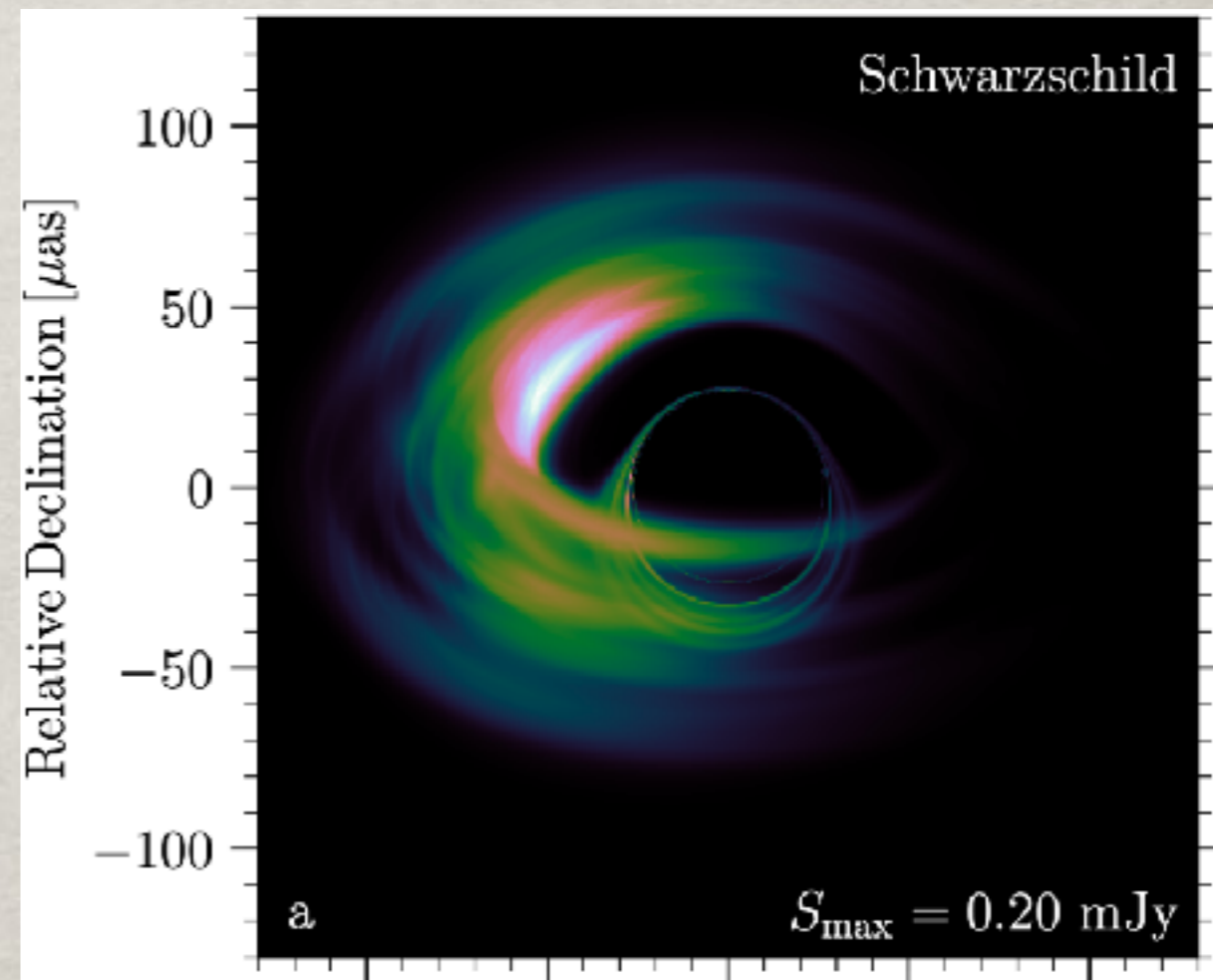
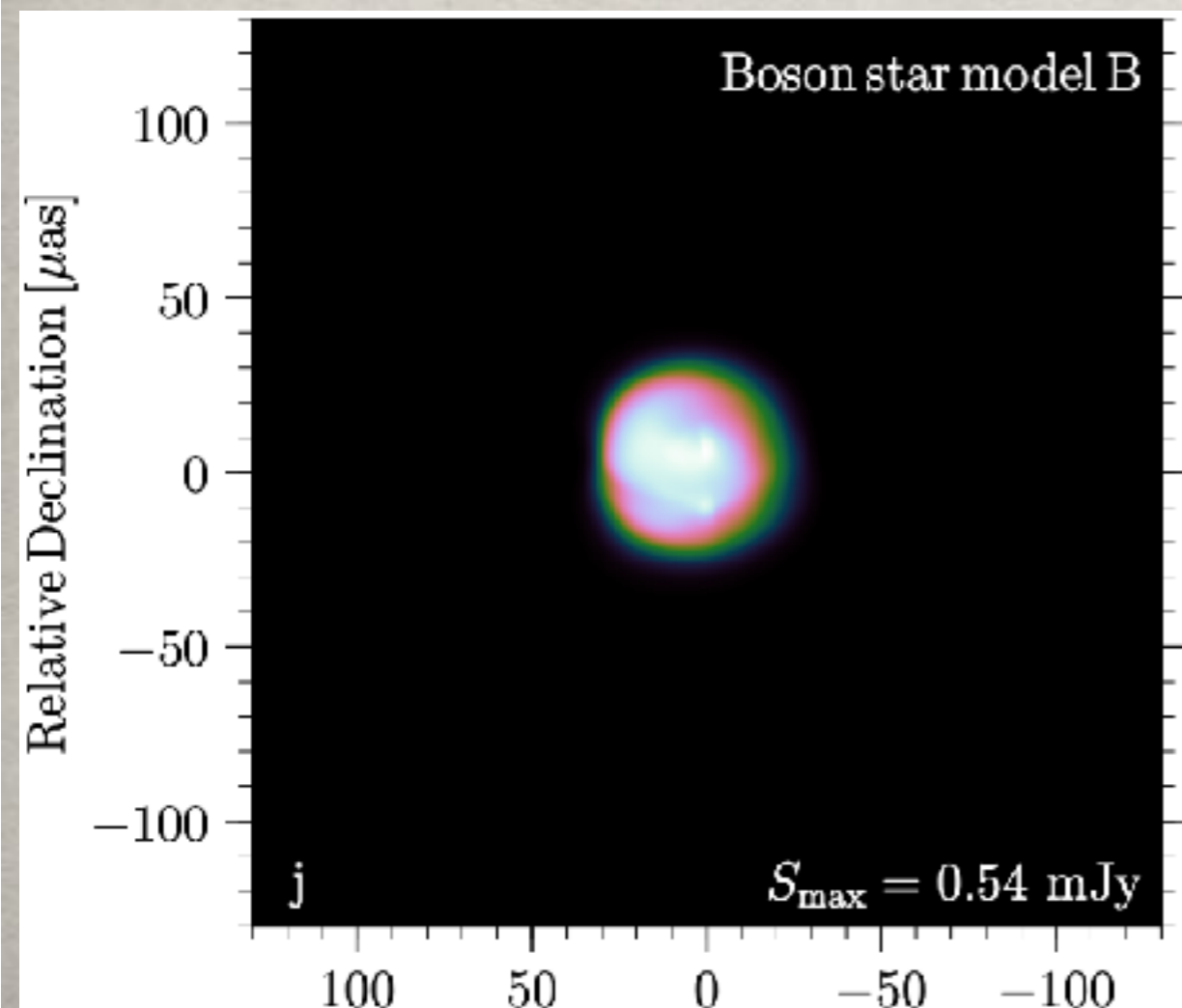
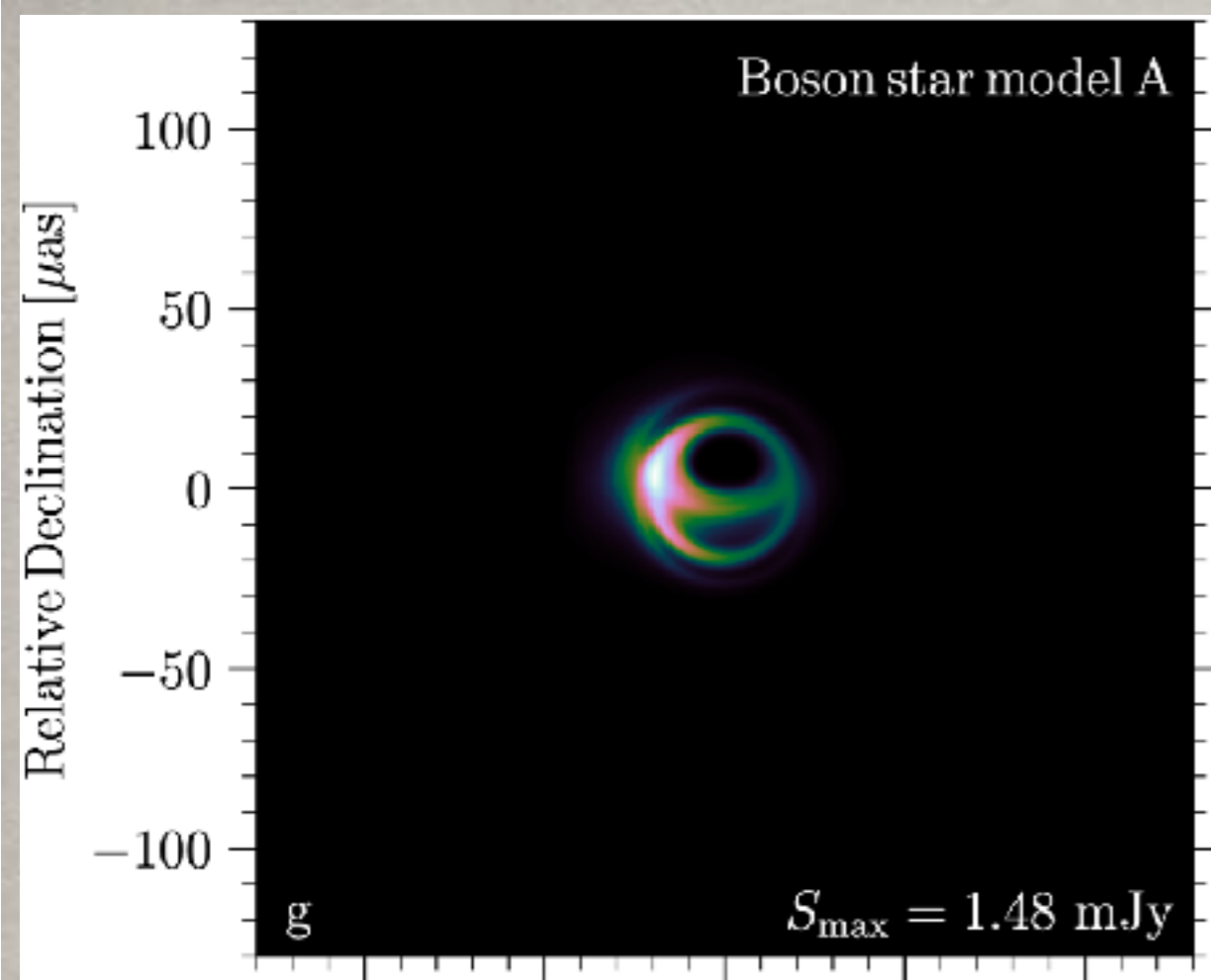
Goebel, Astrophys. J. 172 (1972) L95

Cardoso, Franzin and Pani, PRL 116 (2016) 171101



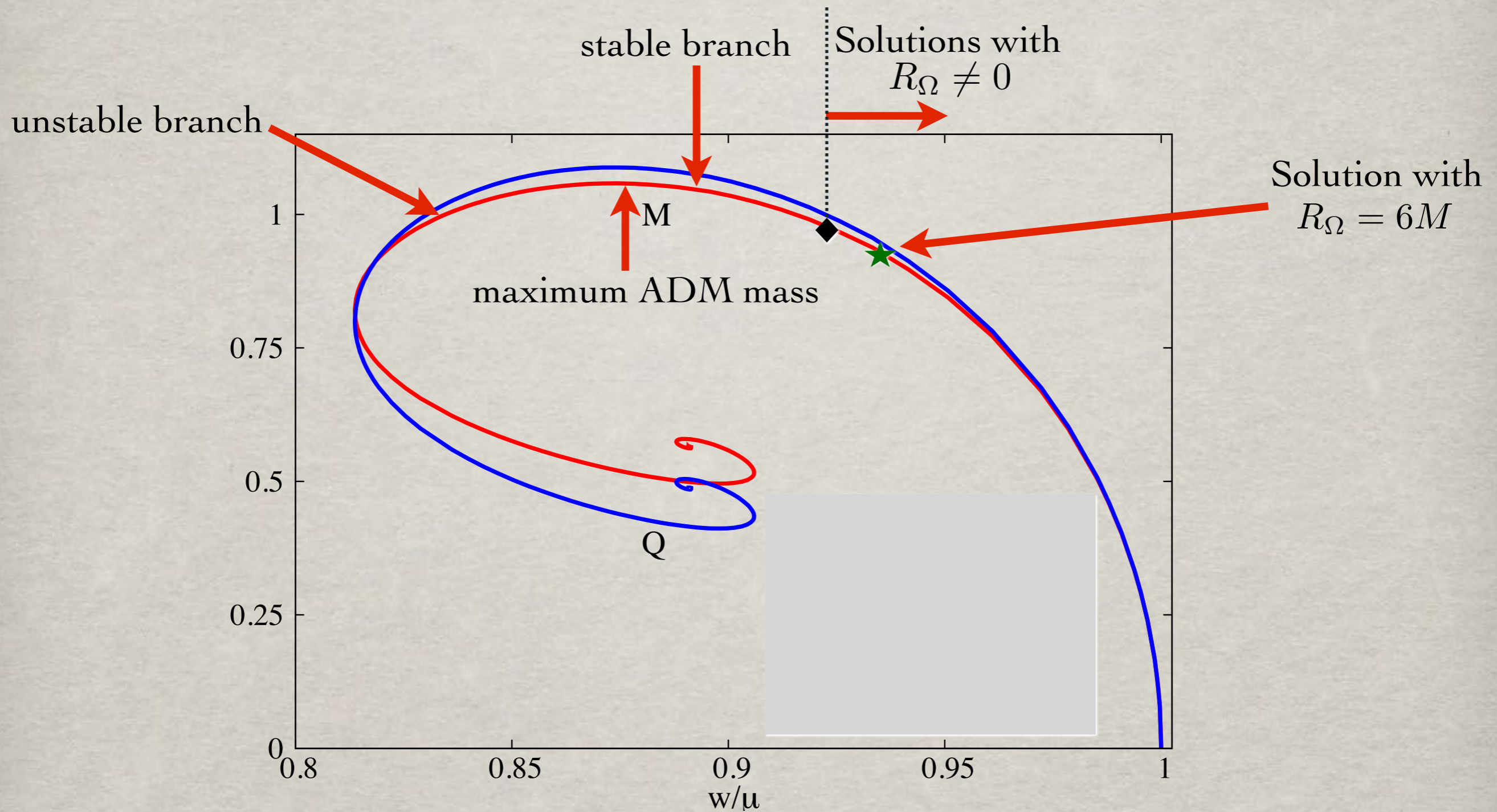
$j \sim 0.82$





Olivares, Younsi, Fromm, De Laurentis, Porth, Mizuno,
Falcke, Kramer, Rezzolla,
Mon. Not. Roy. Astron. Soc. 497 (2020) 521

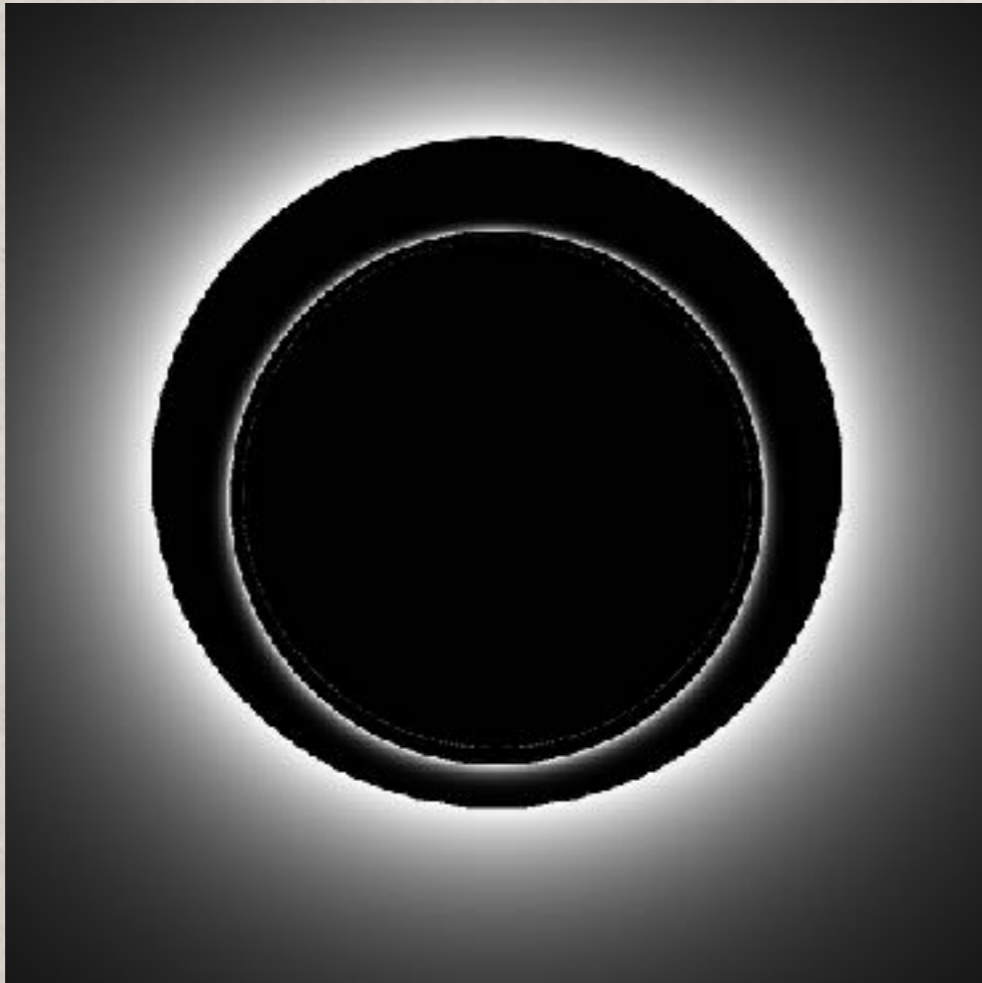
Spherical Proca stars domain of existence



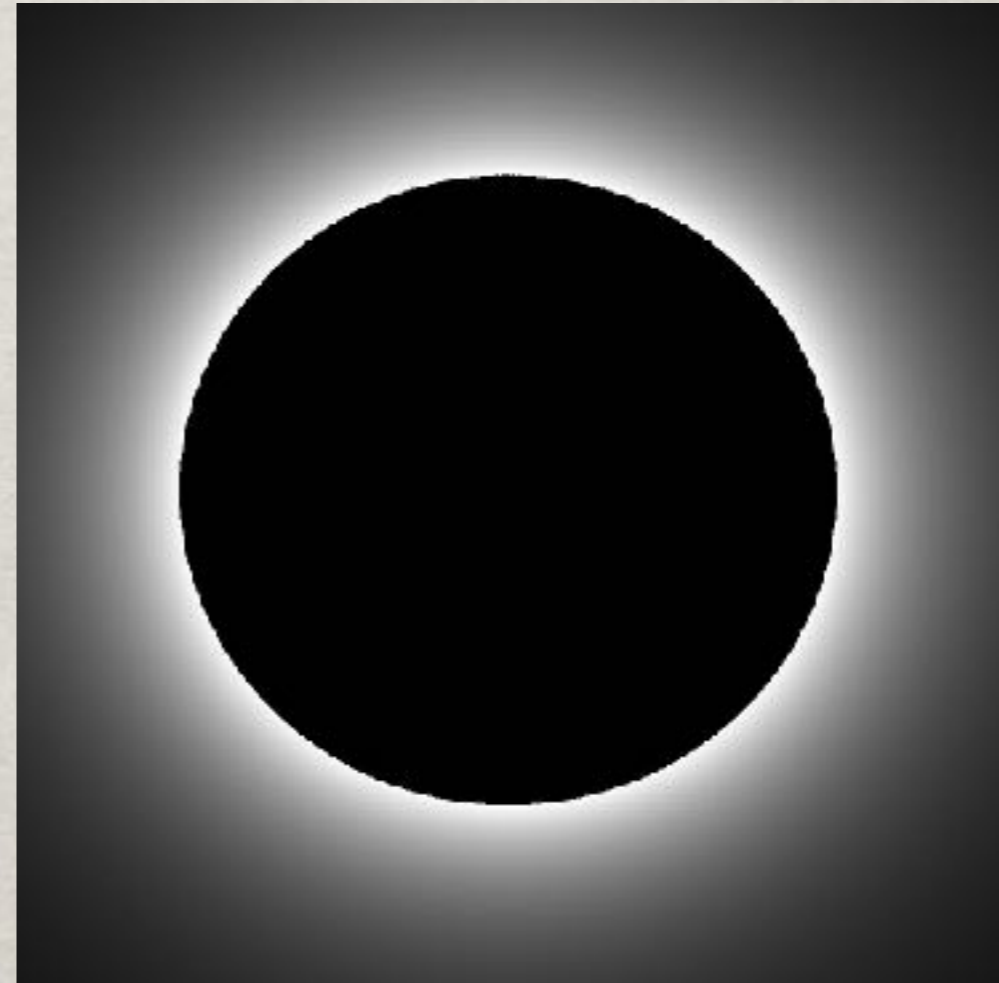
Almost polar observation

$$\theta_{\text{obs}} = 17^\circ \quad r_{\text{obs}} = 100M$$

Schwarzschild BH



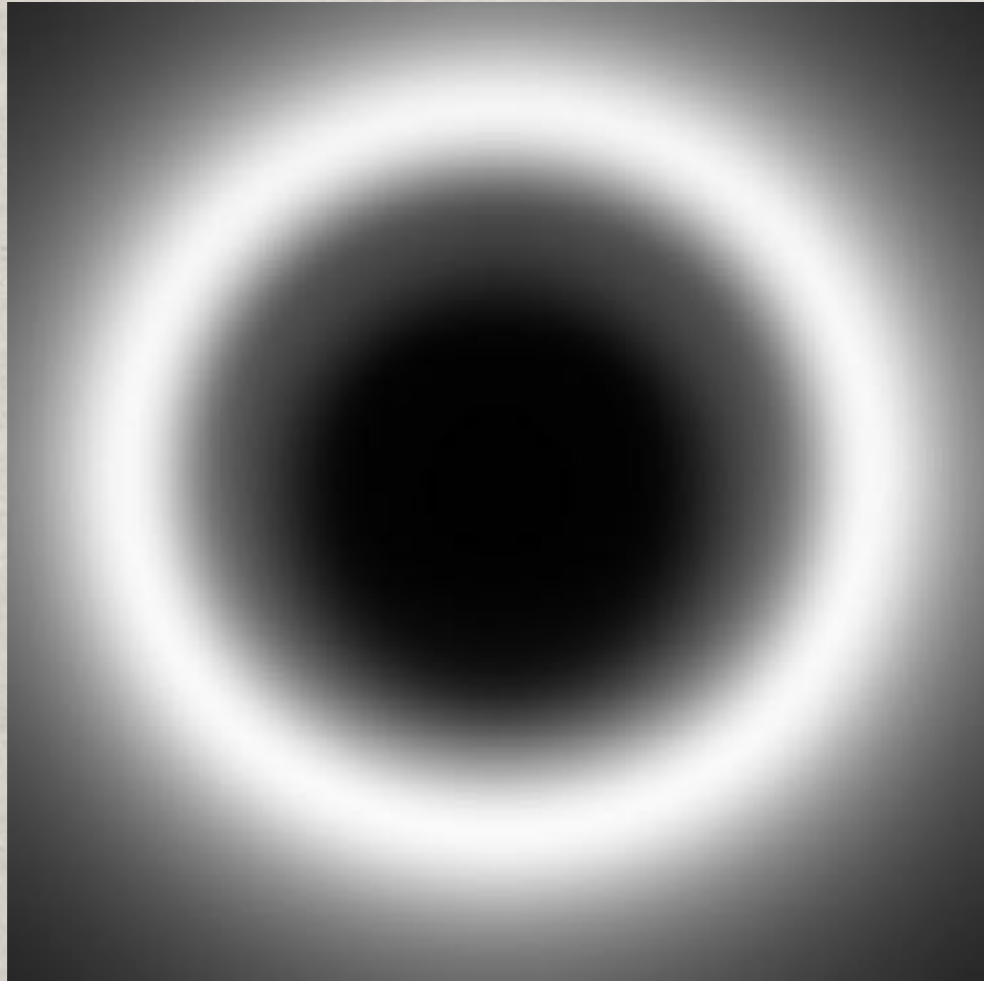
Proca star



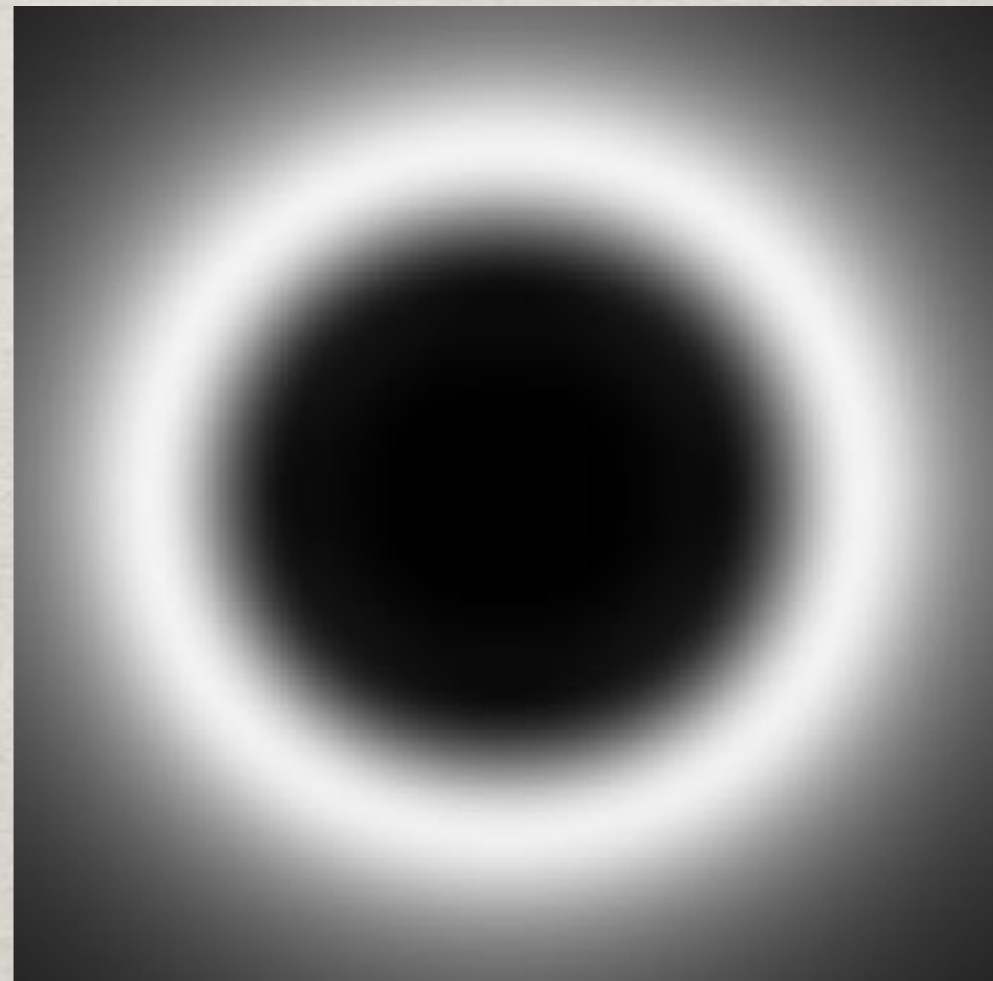
Almost polar observation

$$\theta_{\text{obs}} = 17^\circ \quad r_{\text{obs}} = 100M$$

Schwarzschild BH



Proca star

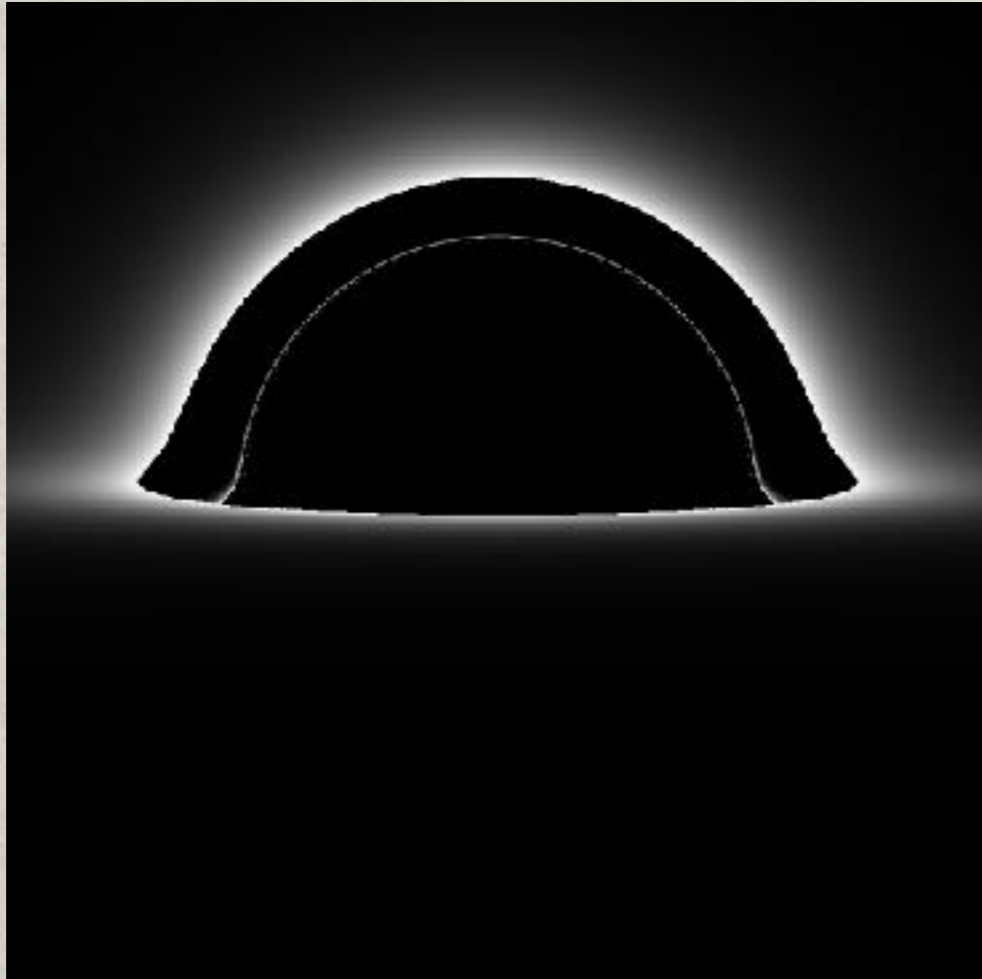


Applying a Gaussian blurring filter

Almost equatorial observation

$$\theta_{\text{obs}} = 86^\circ \quad r_{\text{obs}} = 100M$$

Schwarzschild BH



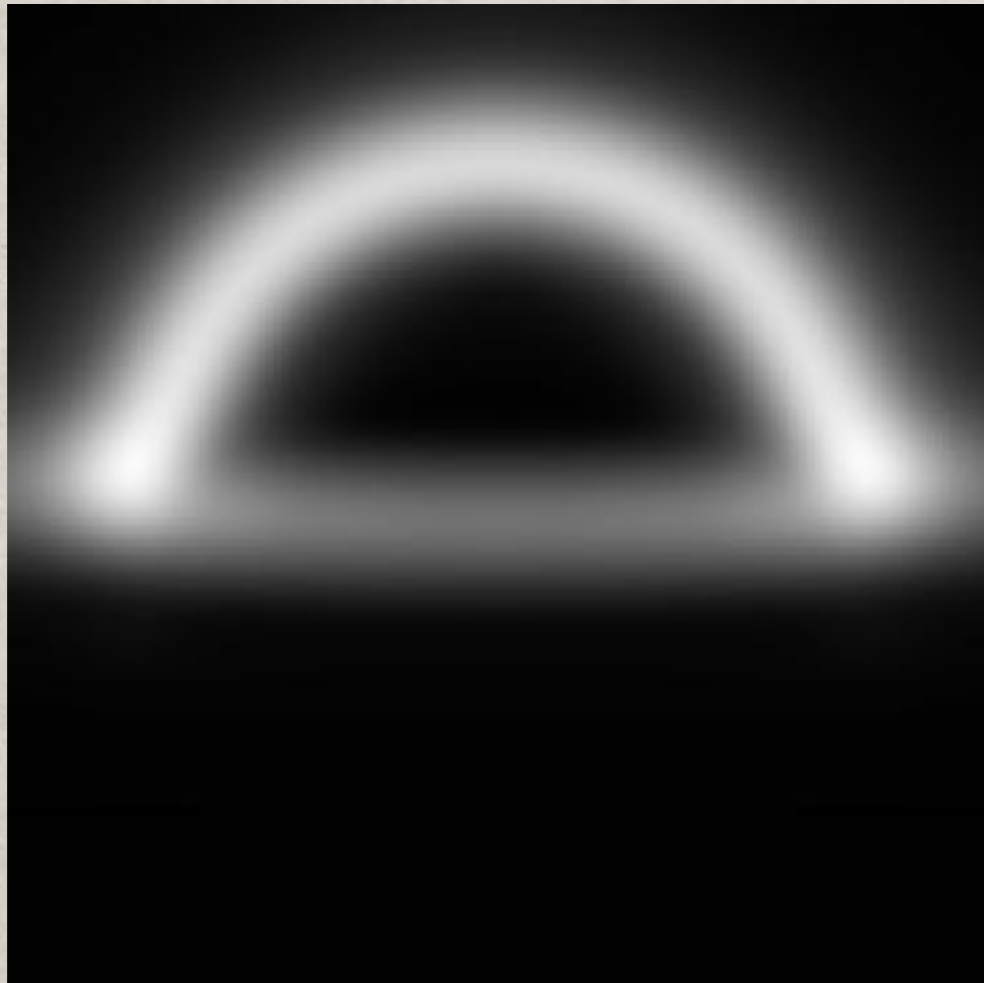
Proca star



Almost equatorial observation

$$\theta_{\text{obs}} = 86^\circ \quad r_{\text{obs}} = 100M$$

Schwarzschild BH



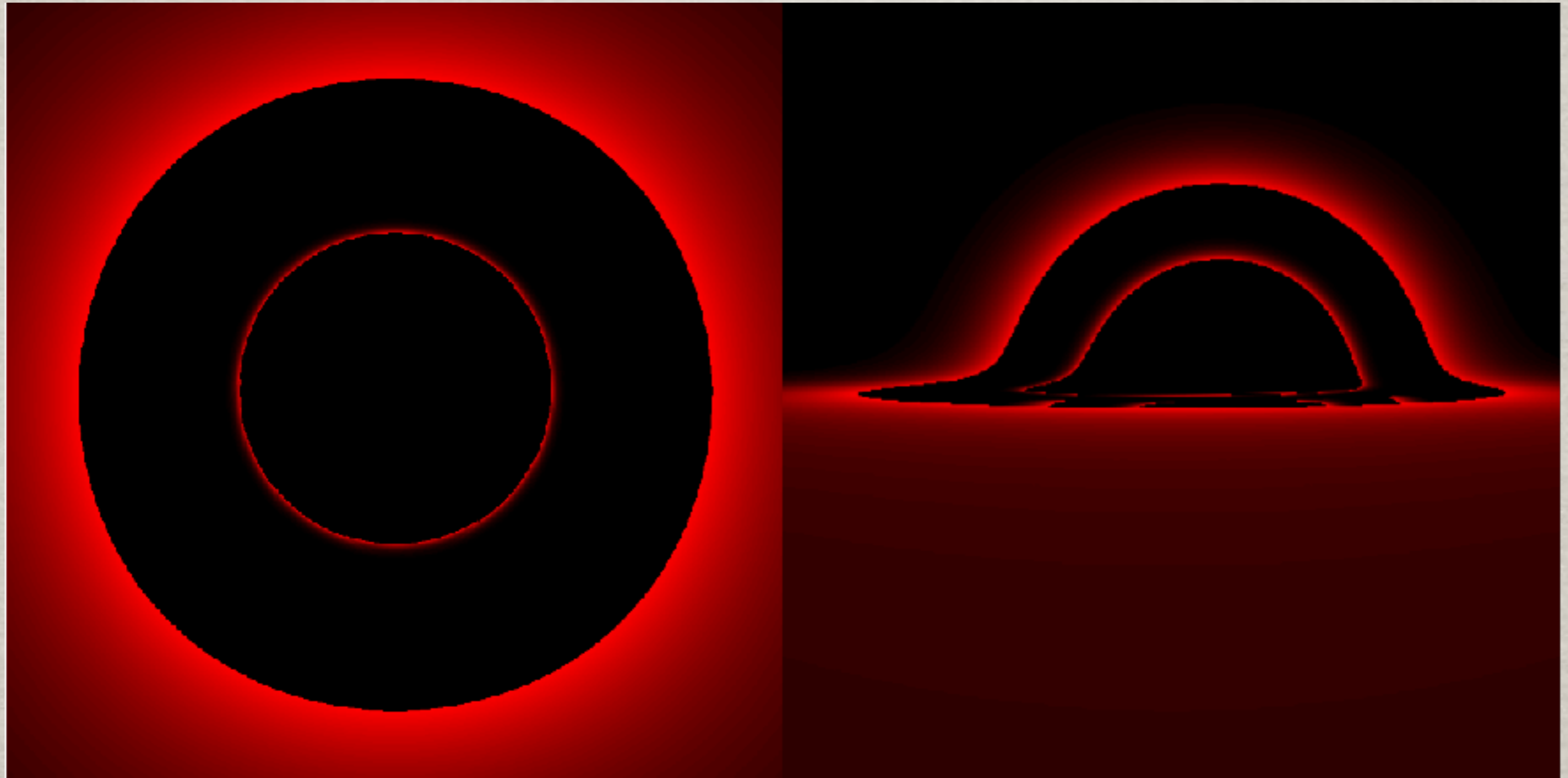
Proca star



Applying a Gaussian blurring filter

The imitation game reloaded

Sengo, Cunha, CH, Radu,
ArXiv: 2402.14919 (to appear in JCAP)



(a) $\theta = 5^\circ$

(b) $\theta = 88^\circ$

Concluding remark:

Bosonic stars illustrate theoretical possibilities of dynamically robust black hole imitators that could manifest themselves only at some specific scales.

Producing detailed phenomenology will constrain the model and the corresponding (exotic) physics or, in the best case scenario, provide a smoking gun to this new physics.

R. Bernar's
and
A. Higuchi
talk's

The wonderful world of compact objects with bosonic fields in GR

Amazonian Workshop

IX

Thank you for your attention!
Muito obrigado pela vossa
atenção

June 17th - 21st 2024

Federal University of Pará

Carlos Herdeiro

Gravitational Geometry and Dynamics Group, Aveiro University, Portugal

IX Amazonian Workshop on Gravity and Analogue Models

June 17, 2024

in collaboration with M. Brito, R. Brito, V. Cardoso, P. Cerda-Duran, P. Cunha, E. Costa-Filho, J. Degollado, J. Font, F. di Giovanni, J. Kunz, A. Moraes, I. Parapechka, E. Radu, N. Sanchis-Gual, N. Santos, Y. Shnir, M. Zilhão,...